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Rainfall Disaggregation Methods: Theory and Applications

Demetris Koutsoyiannis Department of Water Resources, School of Civil Engineering, National Technical University, Athens, Greece









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General purpose stochastic disaggregation: Weaknesses and remediation

Weakness	Remediation	Comments
Independence of consecutive lower- layer variables belonging to consecutive periods	Different model structures, simultaneously involving lower-layer variables of the earlier period	 Use of even larger parameter sets Only partial remediation
Inability to perform with non-Gaussian distribution	Use of nonlinear transformations of variables	Violation of the additive property
	Attempt to preserve the skewness	Infeasibility to preserve large skewness
Excessive number of parameters	 Different model types: Staged disaggregation models Condensed disaggregation models Dynamic disaggregation models 	Better performance compared to the original model types





The two most useful adjusting procedures

1. Proportional adjusting procedure

$$X_s = \widetilde{X}_s \left(Z \,/\, \widetilde{Z} \right)$$

- It preserves exactly the complete distribution functions if variables X_s are independent with two-parameter gamma distribution and common scale parameter
- It gives good approximations for gamma distributed X_s
- 2. Linear adjusting procedure

$$X_s = \widetilde{X}_s + \lambda_s \left(Z - \widetilde{Z} \right)$$

where λ_s are unique coefficients depending of covariances of X_s and Z

- It preserves exactly the complete distribution functions if variables X_s are normally distributed
- It is accurate for the preservation of means, variances and covariances for any distribution of variables X_s

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The general linear coupling transformation for the multivariate case

Mathematical formulation

$$\mathbf{X}_{i}^{*} = \widetilde{\mathbf{X}}_{i}^{*} + \mathbf{h} \left(\mathbf{Z}_{i}^{*} - \widetilde{\mathbf{Z}}_{i}^{*} \right)$$

where

only







Implementation of general-purpose disaggregation models for rainfall disaggregation The disaggregation approach based on the coupling

- The disaggregation approach based on the coupling of models of different timescales can be directly implemented in rainfall disaggregation
- In single variate setting: A point process model, like the Bartlett-Lewis (BL) model, can be used as the lower-level model ⇒ Hyetos
- In multivariate setting there are two possibilities for the lower-level model
 - Use of a multivariate (space-time) extension of a point process model
 - Combination of a detailed single variate model and a simplified multivariate model ⇒ MuDRain The detailed single variate model can be replaced by observed time series if applicable

















MuDRain: A model for multivariate disaggregation of rainfall at a fine time scale

Basic assumptions

- The disaggregation is performed at *n* sites simultaneously
- At all *n* sites there are higher-level (daily) time series available, derived either
 - from measurement or
 - from a stochastic model (daily)
- At one or more of the *n* sites there are lower-level (hourly) series available, derived either
 - from measurement or
 - from a stochastic model (hourly, e.g. Hyetos)
- The lower-level rainfall process at the remaining sites can be generated by a simplified multivariate AR(1) model (X_s = a X_{s-1} + b V_s) utilising the cross-correlations among the different sites

MuDRain = multivariate AR(1) + repetition + coupling transformation

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Can a simple AR(1) model describe the rainfall process adequately? Exploration of the distribution function of hourly rain depths during wet days Data: a 5-year time series of January (95 wet days, 2280 data values) Location: Gauge 1, Brue catchment, SW England Highly skewed 10 distribution Hourly rainfall depth (mm) 73.6% of values (1679 values) are zeros The smallest measured values are 0.2 mm Measured zeros can 0.1 be equivalently Historical regarded as < 0.1 mm - Theoretical - Gamma With this assumption, - 10% limits of Kolmogorov-Smirnov test a gamma distribution 0.01 can be fitted to the 70 80 90 99 95 99.9 99.99 entire domain of the Non-exceedance probability (%) rainfall depth D. Koutsoyiannis, Rainfall disaggregation methods 24

















Hypetos main program form
Next <i>n</i> sequences of wet days
where $n = 10$ Use constant length L of wet day sequences
where $L = 1$
Next sequence of wet days
Initialise Write synthetic data to file
Sequence #: 2 Input file: none Duput file: none
Clear visual output
Define the level of details printed
(0 = few, 3 = many) Print statistics
Show graphs
Edit Bartlett-Lewis model parameters
Edit repetition options
About
Model information - Help
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Conclusions (2) Single-variate versus multivariate models

Simulations

- Current hydrological modelling requires spatially distributed information
- Thus, multivariable rainfall disaggregation models have greater potential as they generate multivariate fields at fine temporal resolution

Enhancement of data records

- Provided that there exists at least one fine resolution raingauge at the area of interest, multivariate models have greater potential to disaggregate daily rainfall at finer time scales, because
 - they can derive spatially consistent rainfall series in number of raingauges simultaneously, in which only daily data are available
 - they can utilise the spatial correlation of the rainfall field to derive more realistic hyetographs

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Conclusions (3) The Hyetos and MuDRain software applications

- Hyetos combines the strengths of a standard singlevariate stochastic rainfall model, the Bartlett-Lewis model, and a general-purpose disaggregation technique
- MuDRain combines the simplicity of the multivariate AR(1) model, the faithfulness of a more detailed singlevariate model (for one location) and the strength of a general-purpose multivariate disaggregation technique
- Soth models are implemented in a user-friendly Windows environment, offering several means for user interaction and visualisation
- Soth programs can work in several modes, appropriate for operational use and model testing

Conclusions (4) Results of case studies using Hyetos and MuDRain

The case studies presented, regarding the disaggregation of daily historical data into hourly series, showed that both Hyetos and MuDRain result in good preservation of important properties of the rainfall process such as

- marginal moments (including skewness)
- temporal correlations
- proportions and lengths of dry intervals
- distribution functions (including distributions of maxima)
- In addition, the multivariate MuDRain provides a good reproduction of
 - spatial correlations
 - actual hyetographs





This presentation is available on line at http://www.itia.ntua.gr/e/docinfo/570/ Programs Hyetos and MuDRain are free and available on the web at http://www.itia.ntua.gr/e/softinfo/3/ and http://www.itia.ntua.gr/e/softinfo/1/ The references shown in the presentation can be found in the Workshop proceedings