# European Geosciences Union General Assembly 2007, Vienna, Austria, 15-20 April 2007

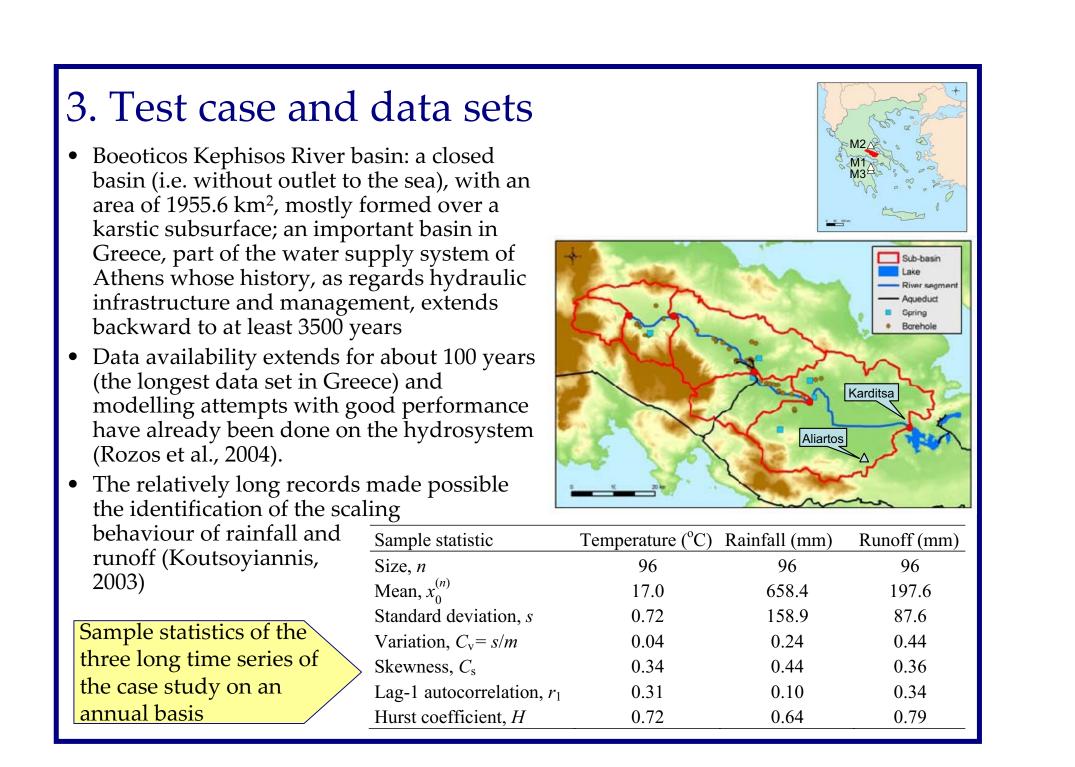
# A stochastic methodological framework for uncertainty assessment of hydroclimatic predictions

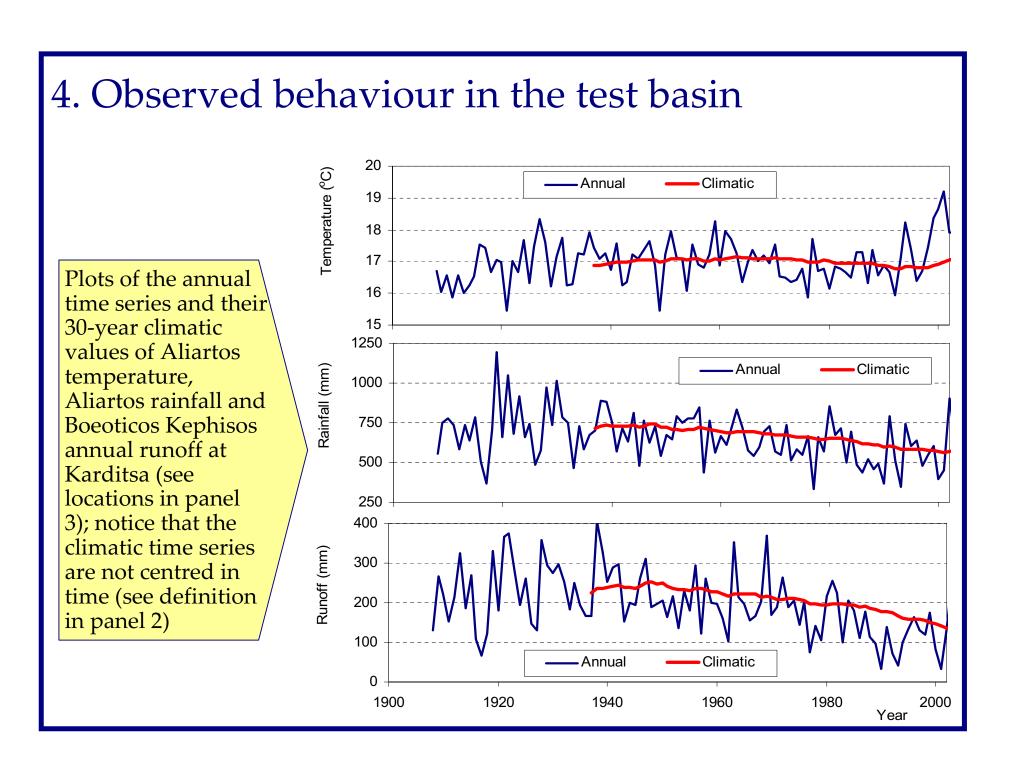
# . Abstract

In statistical terms, the climatic uncertainty is the result of at least two factors, the climatic variability and the uncertainty of parameter estimation. Uncertainty is typically estimated using classical statistical methodologies that rely on a time independence hypothesis. However, climatic processes are not time independent but, as evidenced from accumulating observations from instrumental and paleoclimatic time series, exhibit long-range dependence, also known as the Hurst phenomenon or scaling behaviour. A methodology comprising analytical and Monte Carlo techniques is developed to determine uncertainty limits for the nontrivial scaling case. It is shown that, under the scaling hypothesis, the uncertainty limits are much wider than in classical statistics. Also, due to time dependence, the uncertainty limits of future are influenced by the available observations of the past. The methodology is tested and verified using a long instrumental meteorological record, the mean annual temperature at Berlin. It is demonstrated that the developed methodology provides reasonable uncertainty estimates whereas classical statistical uncertainty bands are too narrow. Furthermore, the framework is applied with temperature, rainfall and runoff data from a catchment in Greece, for which data exist for about a century. The uncertainty limits are then compared to deterministic projections up to 2050, obtained for several scenarios from several climatic models combined with a hydrological model. Climatic model outputs for rainfall and the resulting runoff do not display significant future changes as the projected time series lie well within uncertainty limits assuming stable climatic conditions along with a scaling behaviour.

# 2. Rationale and main hypotheses

- Climate is not constant but rather varying in time and expressed by the long-term (e.g. 30-year) time average of a natural process, defined on a fine scale; • The evolution of climate is represented as a stochastic process; if  $X_i$  denotes an
- atmospheric or land surface variable at the annual scale, then climate is represented by the moving average process, with a typical time window k = 30:  $X_i^{(k)} := (X_i + \dots + X_{i-k+1})/k$
- The distributional parameters of the process, marginal and dependence, are estimated from an available sample by statistical methods
- The climatic uncertainty is the result of at least two factors, the climatic variability and the uncertainty of parameter estimation (sampling uncertainty) • A climatic process exhibits scaling behaviour, also known as long-range
- dependence, multi-scale fluctuation or the Hurst phenomenon (Koutsoyiannis, 2002, 2003, 2005); this has been verified both in long instrumental hydrometeorological (and other) series and proxy data
- Because of the dependence, the uncertainty limits of the future are influenced by the available observations of the past
- Future climate trends suggested by general circulation models (GCM) should be viewed in the framework of uncertainty bands estimated by statistics accounting for scaling behaviour





- for confidence coefficient  $\alpha$ :
- confidence coefficient  $\alpha'$ :
- above

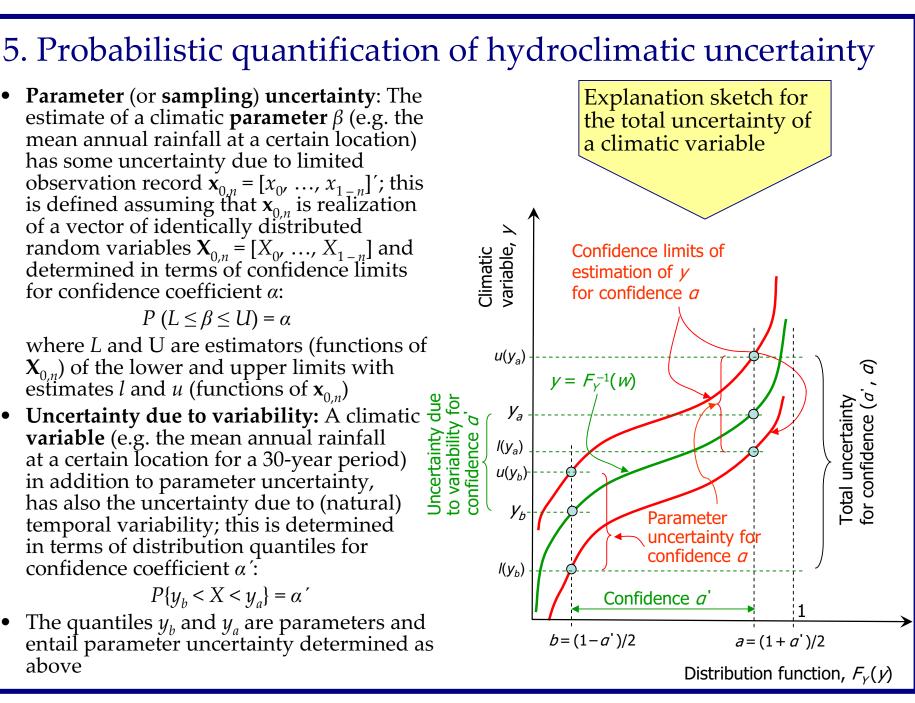
- fundamental law
- of X:
- the Hurst coefficient • The latter law:
- behaviour);

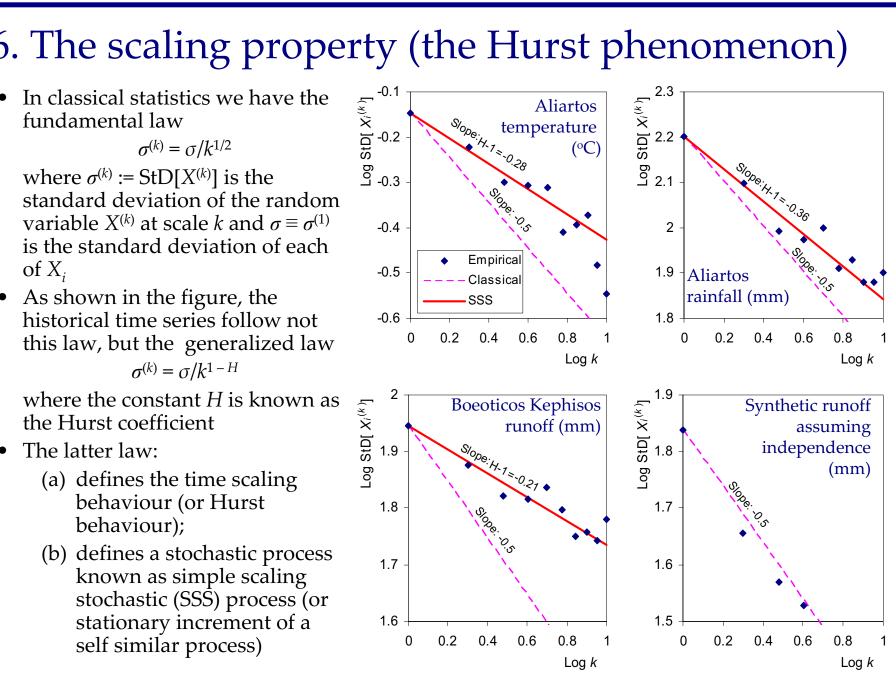
# (close to expectation)

respectively

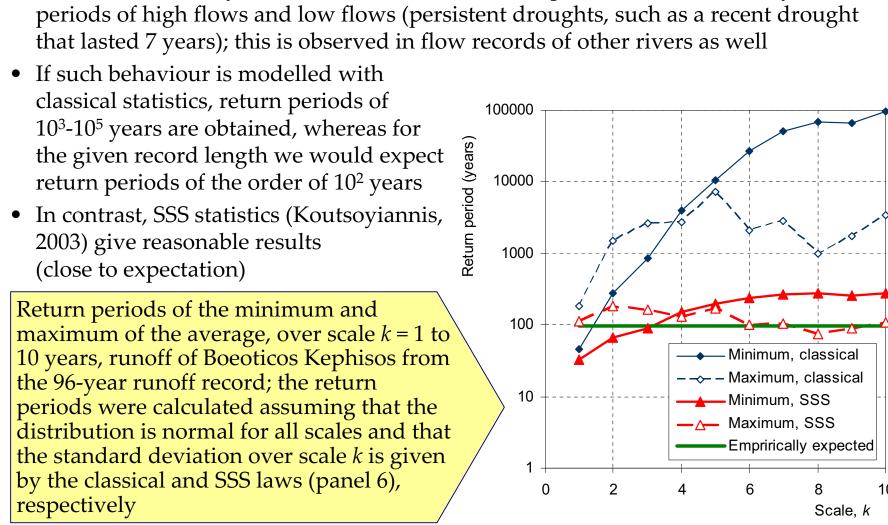
8.	Uncon
•	For confiden <b>due to varia</b> assuming no
•	where $\zeta_b$ is the obtained for The <b>parameter</b> Assuming the being equal $\gamma$ analytical ex $u(y_b^{(k)})$ and $l(y_b^{(k)})$
	E,
•	It can be ver expressions

D. Koutsoyiannis and Andreas Efstratiadis, Department of Water Resources, National Technical University of Athens, Greece Konstantine P. Georgakakos, Hydrologic Research Center, San Diego, CA., USA





## The importance of the scaling behaviour in typical hydrological tasks • In the observed 96-year flow record of Boeoticos Kephisos, there are multi-year



# nditional uncertainty for the SSS case

ence coefficient  $\alpha'$ , the distribution quantiles of  $X_i^{(k)}$  defining the **uncertainty ability** are  $y_h^{(k)}$  and  $y_a^{(k)}$  where  $b = (1 - \alpha')/2$ ,  $a = (1 + \alpha')/2$ ; for the SSS case ormal distribution, these are given as

 $y_{b}^{(k)} = \mu + \zeta_{b} \sigma / k^{1-H}$ 

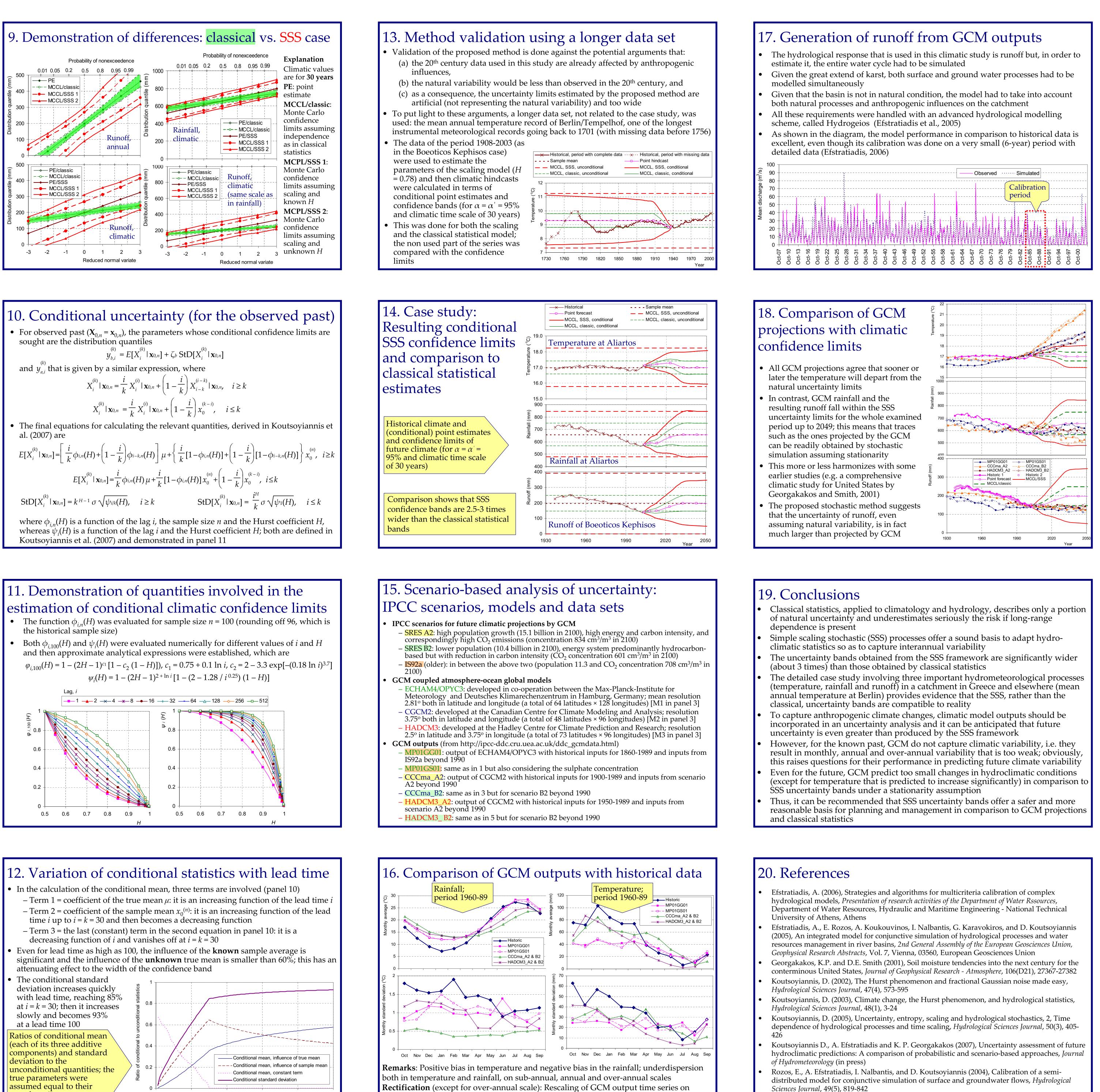
the *b* quantile of the standard normal distribution; a similar expression is

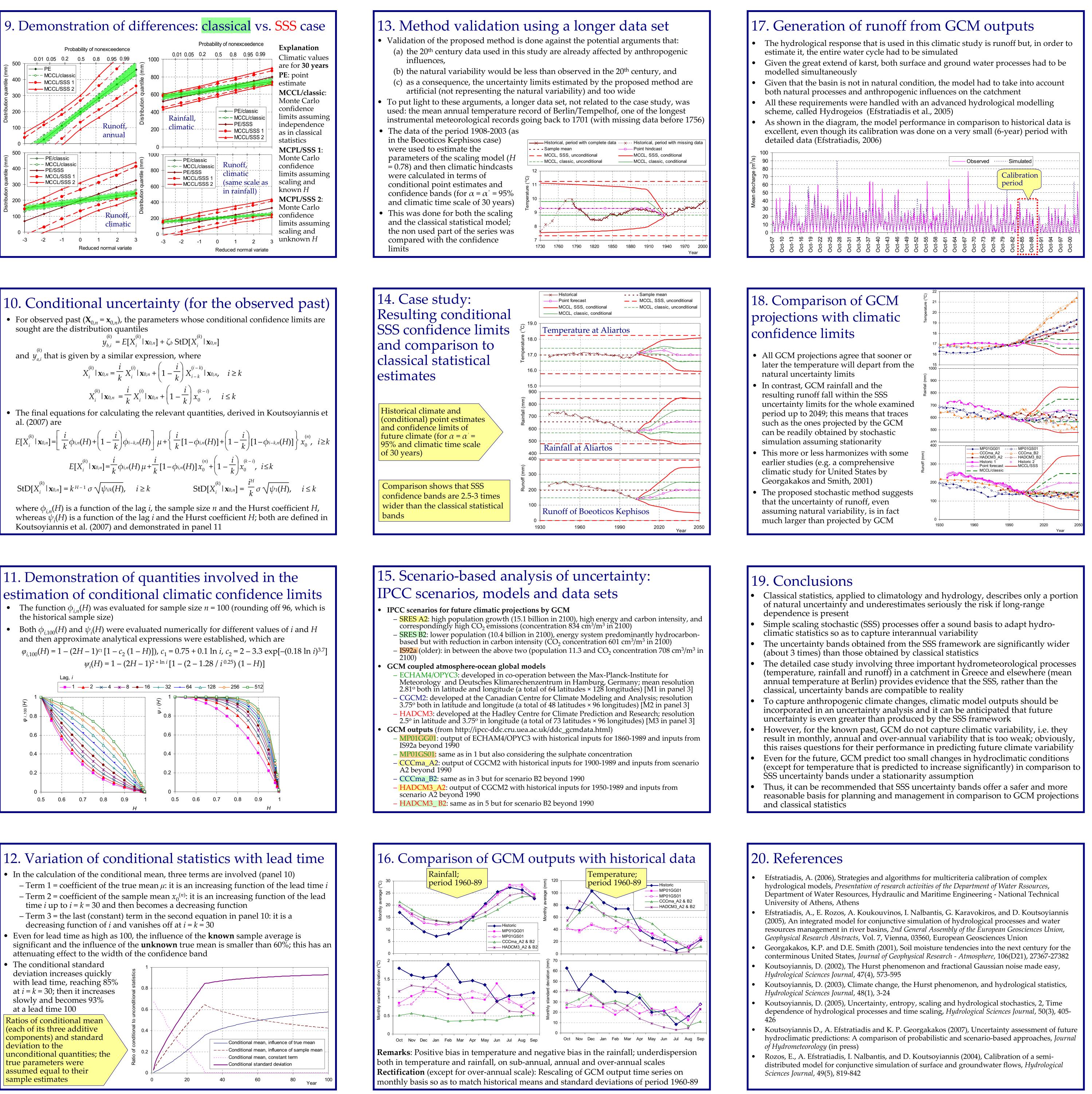
**eter uncertainty** is due to uncertainty in the estimation of  $\mu$ ,  $\sigma$  and Hthat the true values of  $\sigma$  and H are known without uncertainty (the former l to the sample estimate *s* of standard deviation), the following semixpressions have been derived for the upper and lower *a*-confidence limits  $l(y_{h}^{(k)})$  of  $y_{h}^{(k)}$  for the SSS case (Koutsoyiannis, 2003):  $u(y_{b}^{(k)}), l(y_{b}^{(k)}) = x_{0}^{(n)} + \zeta_{b} s / k^{1-H} \pm \zeta_{(1+\alpha)/2} \varepsilon_{b} s$ 

 $\varepsilon_b = \frac{1}{n^{1-H}} \sqrt{1 + \frac{\varphi(n, H)}{2 n^{2H-1}} \left(\frac{\zeta_b}{k^{1-H}}\right)^2}, \quad \varphi(n, H) = (0.1 \ n + 0.8)^{0.088(4H^2 - 1)^2}$ 

rified that if H = 0.5 (independence case), these switch to known s in classical statistics; as H grows away from 0.5 the differences from the classical statistics increase drastically

In the more realistic case that all  $\mu$ ,  $\sigma$  and H are unknown and estimated from the sample, the confidence limits can be estimated numerically by Monte Carlo simulation





# Session NP4.02 Statistical analysis of paleoclimate time series