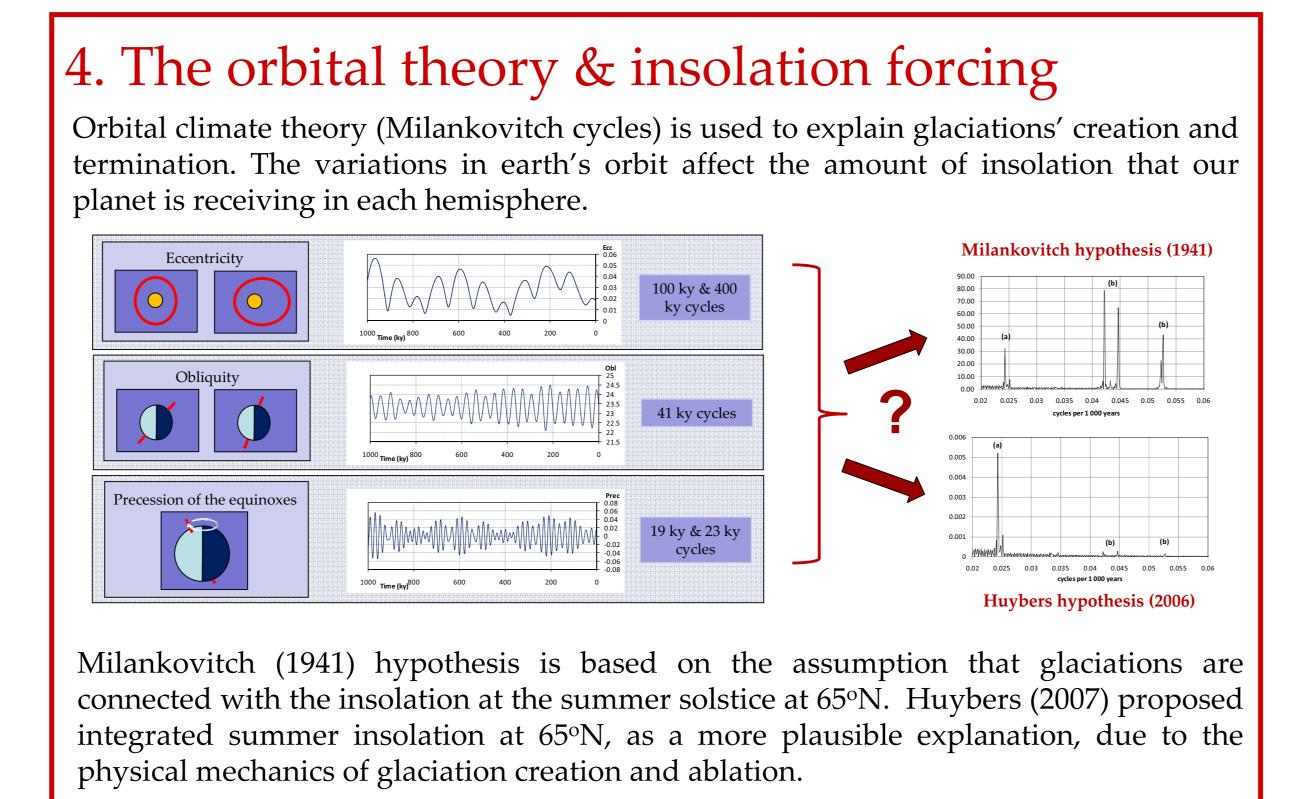
Hurst-Kolmogorov dynamics in long climatic proxy records

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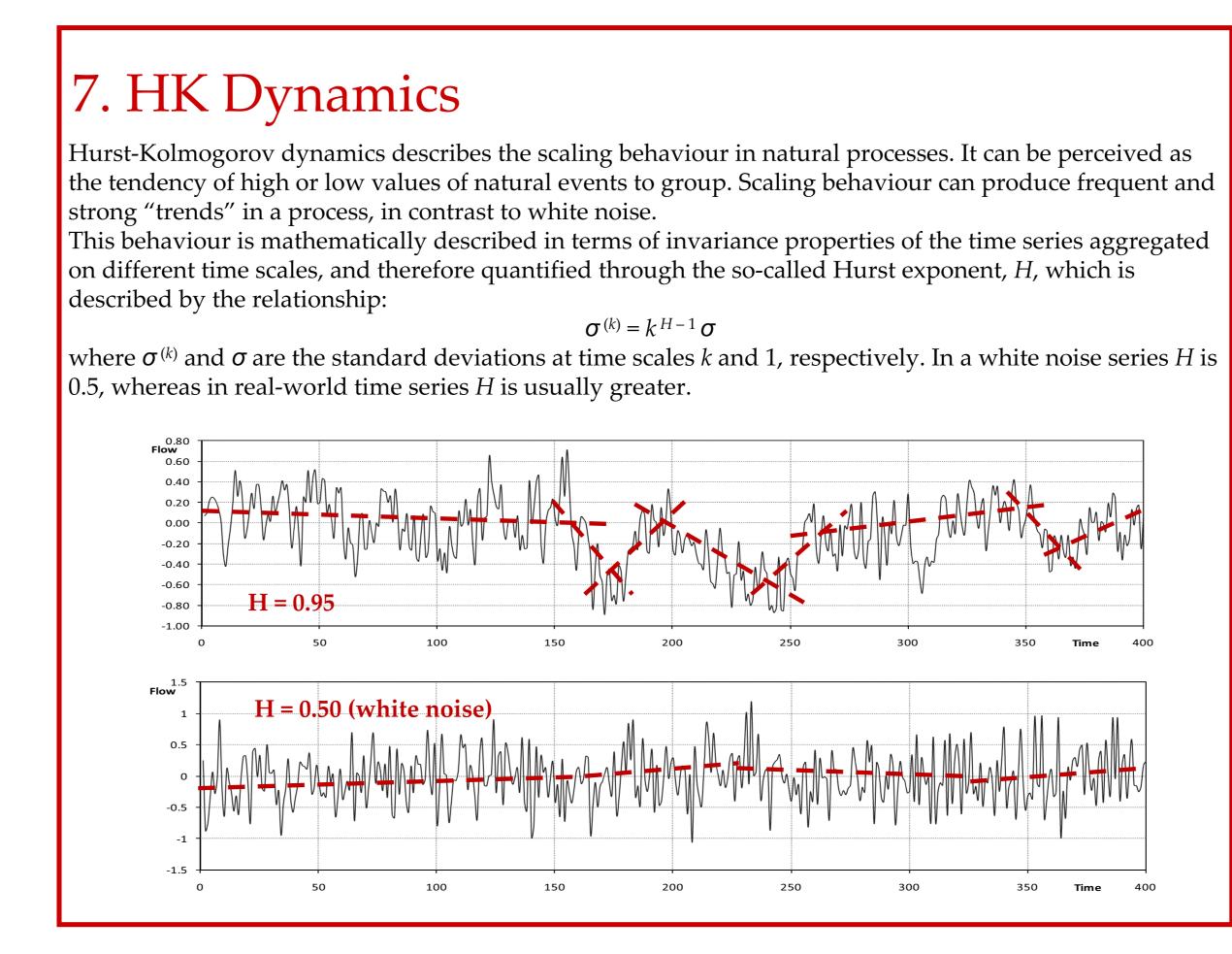
1. Abstract

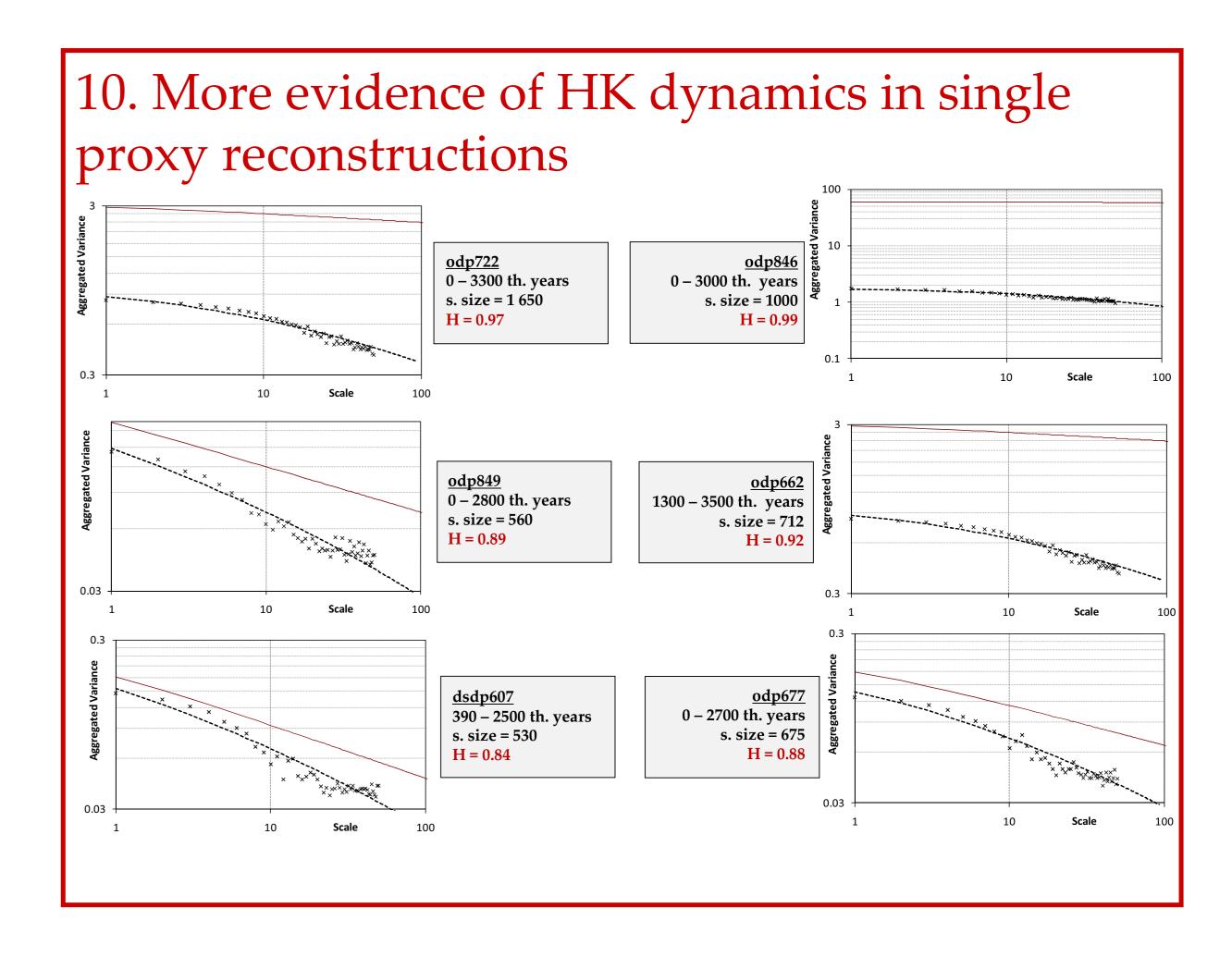
Orbital climate theory states that the variations in insolation caused by changes in the shape of the earth's orbit (eccentricity of ellipse), tilt of the earth's axis (obliquity) and precession of the equinoxes are linked with large-scale climate variations. However, there is an on-going debate about the qualitative characteristics that describe the driving force of large scale climate dynamics (linear vs. nonlinear, insolation vs. obliquity forcing), that extends to a greater disagreement about the overall appropriateness of deterministic or stochastic descriptions of glacial cycles. Through this scientific discussion some concepts are widely used by all sides, including threshold mechanisms, state transition and multi-scale fluctuations, which are characteristics that can be associated with a power-law stochastic dependence. Hurst-Kolmogorov (HK) dynamics is a characteristic model that results in power-law dependence. Here we show that HK dynamics combined with components of orbital forcing is consistent with several proxy climatic time series spanning periods up to 500 million years before present.



Huybers hypothesis focuses on the role of obliquity forcing, whereas Milankovitch

theory is precession-oriented.

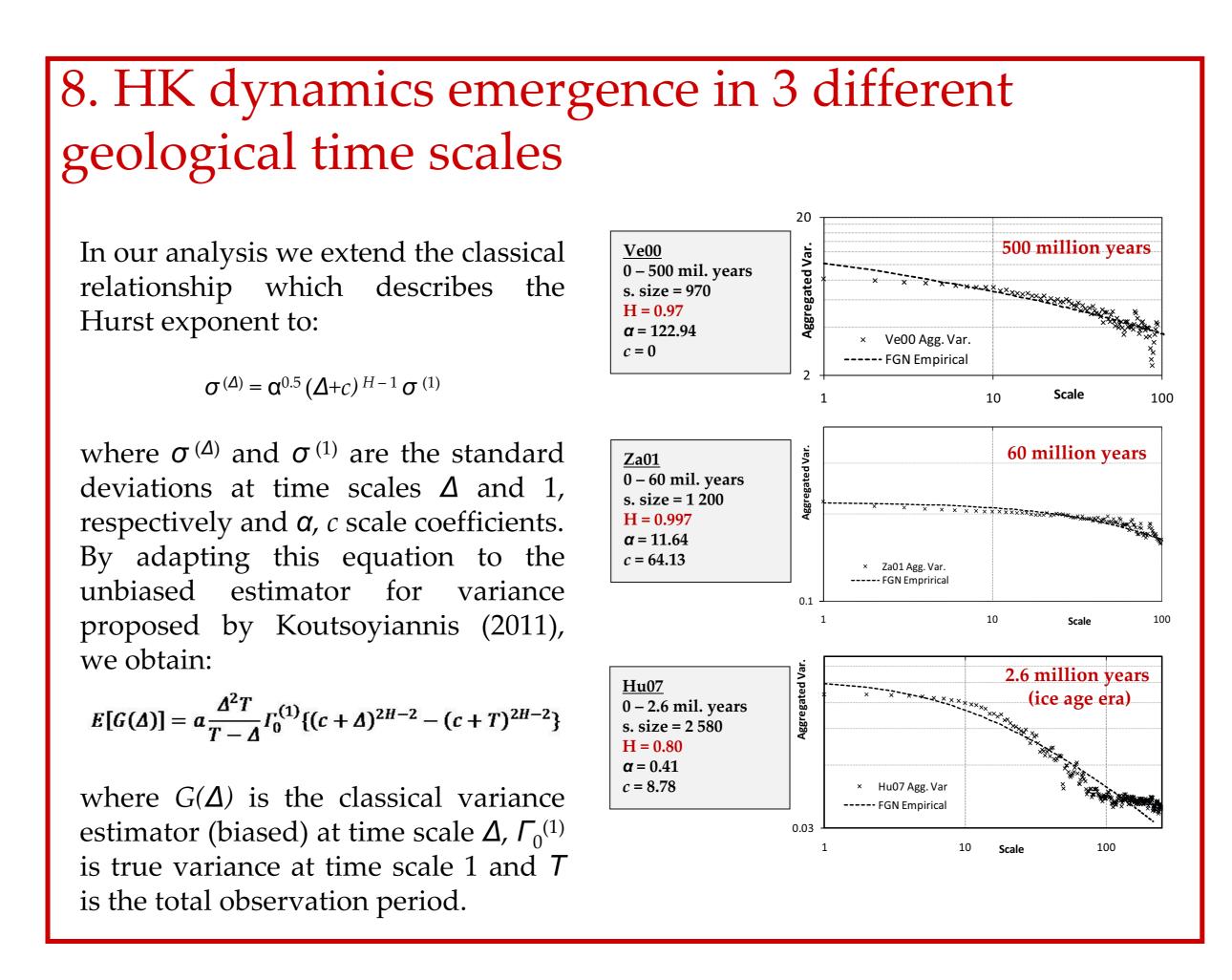




2. Motivation

- There is an on-going debate about the consistency of orbital climate theory, based on some contradictions between the results of this theory and paleoclimatic data.
- In this debate, extensive use of the well-known rules of classical statistics is typically made. The Hurst-Kolmogorov approach provides a better representation of the basic statistical properties of empirical data, such as variance over different scales and autocorrelation function, as long as they indicate long-term persistence.
- Comparison between the statistical estimators of classical statistics (CS) and Hurst-Kolmogorov statistics (HKS), has shown that in these cases the variance and, therefore, the system uncertainty is underestimated by the CS (Koutsoyiannis & Montanari, 2007). This difference becomes quite serious as the Hurst coefficient, which is the index of long-term persistence strength, approaches 1.
- Temperature reconstructions of shorter scales exhibit this kind of behaviour as demonstrated e.g. by Koutsoyiannis (2003); therefore, we investigate possible HK behaviour in longer time scales.

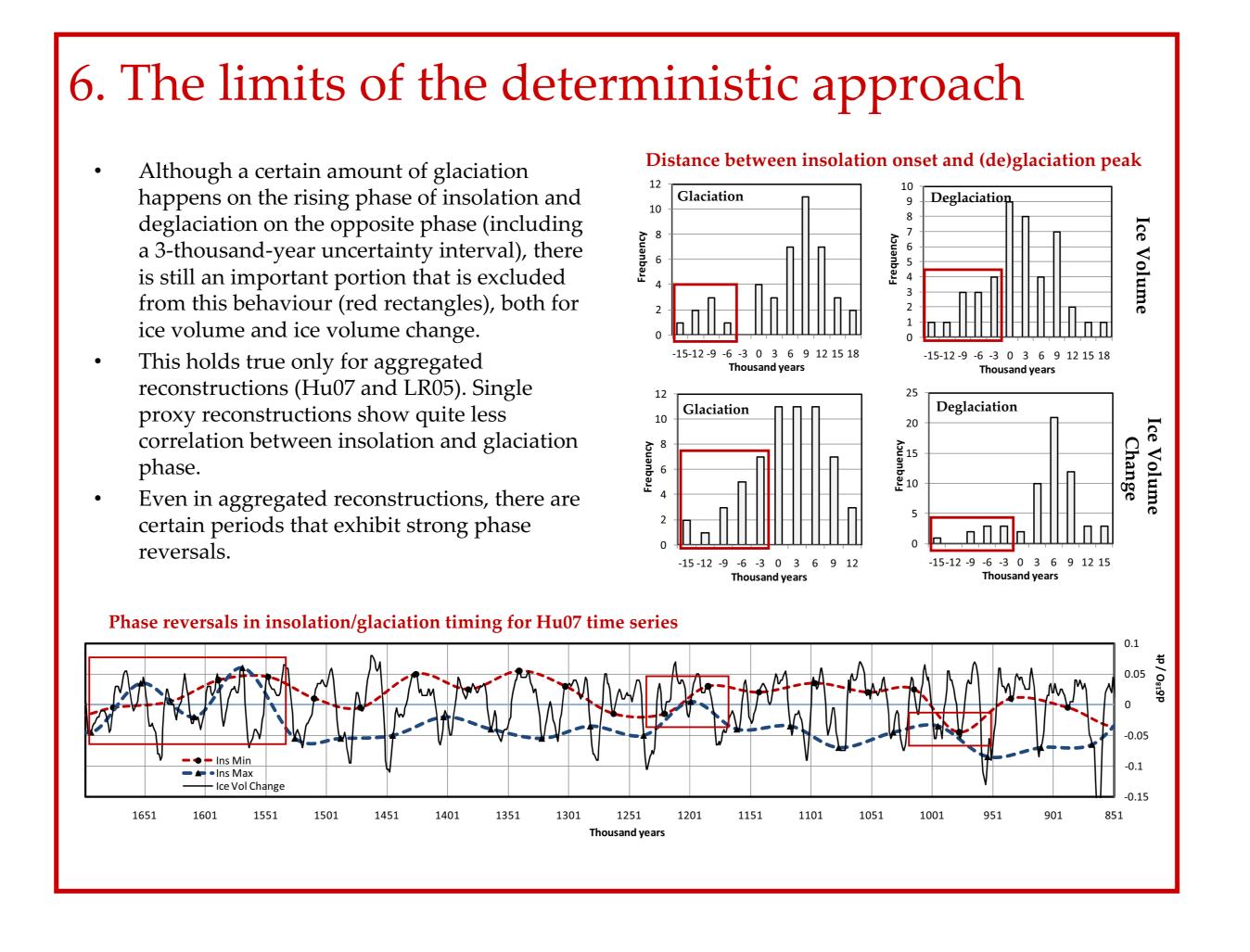
5. Autocorrelation ACF of $\underline{\mathbf{y}}_{i}$ for different values of $\boldsymbol{\alpha}$ We introduce a random variable $\underline{y}_i = \underline{x}_i - \underline{x}_{i-\alpha}$, where a is The variance of autocorrelation function (ACF) of a periodic process with frequency $1/\kappa$ will be minimized for $\alpha = \kappa$, whereas the periodicity will remain for other 500 1000 1500 2000 2500 thousand years The ACF of all paleoclimatic reconstructions of the ice age era, is minimized near 2 obliquity cycles, while it is also low just for one obliquity cycle. An explanation for this could be found in the fact that the 85 000-year cycle is affected also by the precession cycle, in quite a slighter way though. Integrated summer insolation (Huybers hypothesis), follows a similar pattern, while daily insolation does not (Milankovitch theory). 60 80 100 120 140

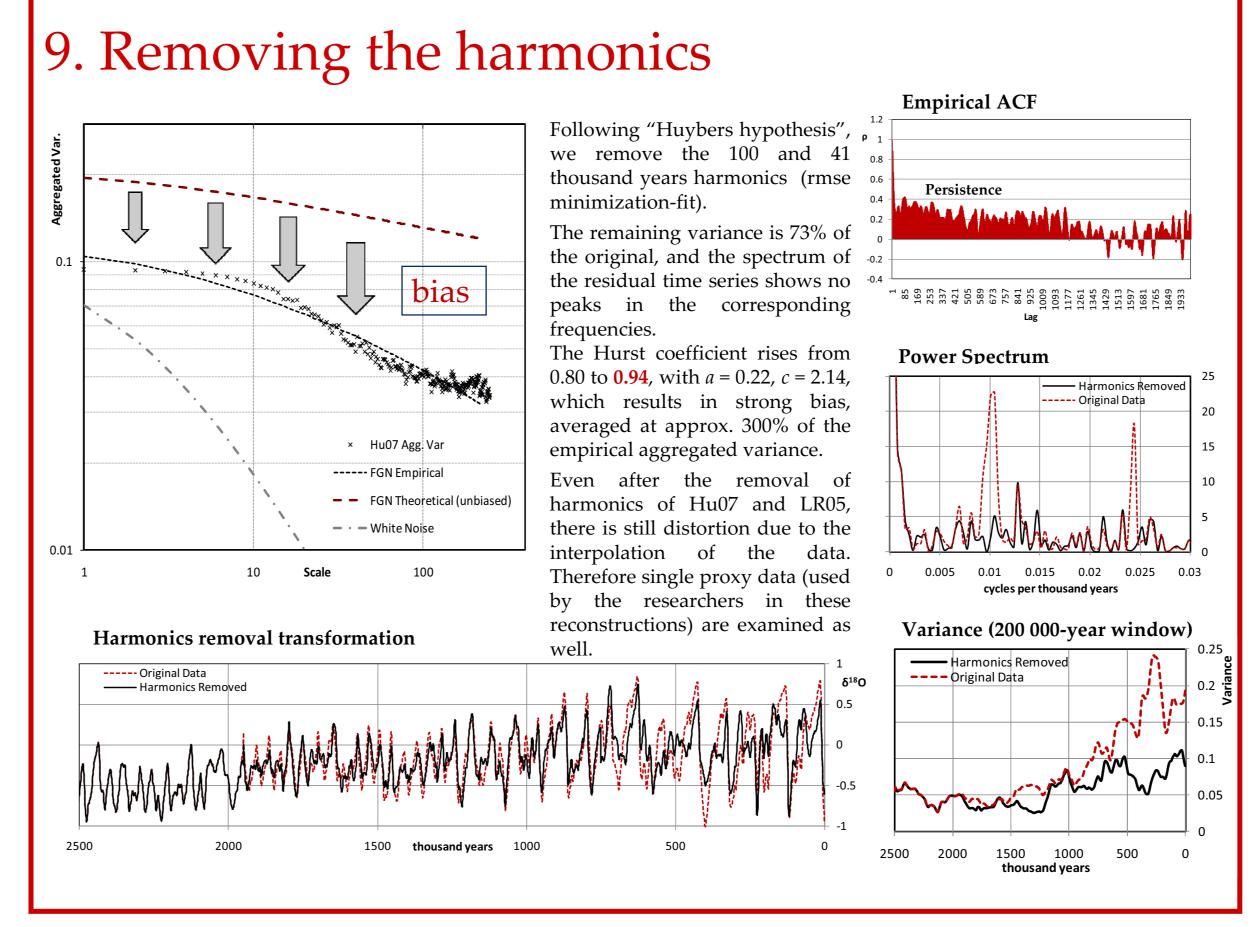


11. Conclusions

- We propose that self-sustained internal variability of the climate system interacts at multi-millennial scales with external forcing described by deterministic cycles of orbital origin.
- These deterministic signatures, evident in time scales between 300 to 3000 thousand years, are explained in a more satisfactory way by the "Huybers hypothesis" than the traditional "Milankovitch theory". They contribute only 30% to system variance, though, leaving 70% of variance often misinterpreted as white noise.
- The deterministic approach has some certain limits, even in the well-studied "Ice age era". Sometimes the glaciers retreat before a corresponding rise in insolation; while in other circumstances the onset of glaciation precedes the insolation fall. The same holds true for the ice volume rate of change.
- On the other hand, internal climatic variability can be described satisfactorily by HK dynamics, a stochastic process that results in power-law dependence, in scales ranging from 1 to 500 million years.
- HK dynamics has been identified in both aggregated and single proxy data, while the addition of deterministic components (orbital harmonics) has a relatively minor impact (≈ 15%) to the estimate of the Hurst coefficient.

3. The Data Set The proxy data were of sediment origin, both of planktic and benthic All reconstructions were interpolated to lower resolution, except Hu07, because of the variable temporal resolution of the In Hu07 though, interpolation was performed by author (Huybers, Hu07 age model was the only one which was not orbitally-tuned and therefore was used for validation Power spectrum was computed by a java FFT algorithm (www.ee.ucl.ac.uk/~mflanaga/java/) cycles per million years





12. References

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