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Application of stochastic methods for wind speed forecasting and wind turbines design at the area of Thessaly, Greece.

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"The answer my friend is blowin' in the wind"
from Bob Dylan's song released in 1962

1. Abstract - Introduction

Several methods exist for estimating the statistical properties of wind speed, most of them being deterministic or probabilistic, disregarding though its long-term behaviour. Here, we focus on the stochastic nature of wind. After analyzing several historical timeseries at the area of interest (AoI) in Thessaly (Greece), we show that a Hurst-Kolmogorov (HK) behaviour is apparent. Thus, disregarding the latter could lead to unrealistic predictions and wind load situations, causing some impact on the energy production and management. Moreover, we construct a stochastic model capable of preserving the HK behaviour and we produce synthetic timeseries using a Monte-Carlo approach to estimate the future wind loads in the AoI. Finally, we identify the appropriate types of wind turbines for the AoI (based on the IEC-61400 standards) and propose several industrial solutions.

2. Area of interest

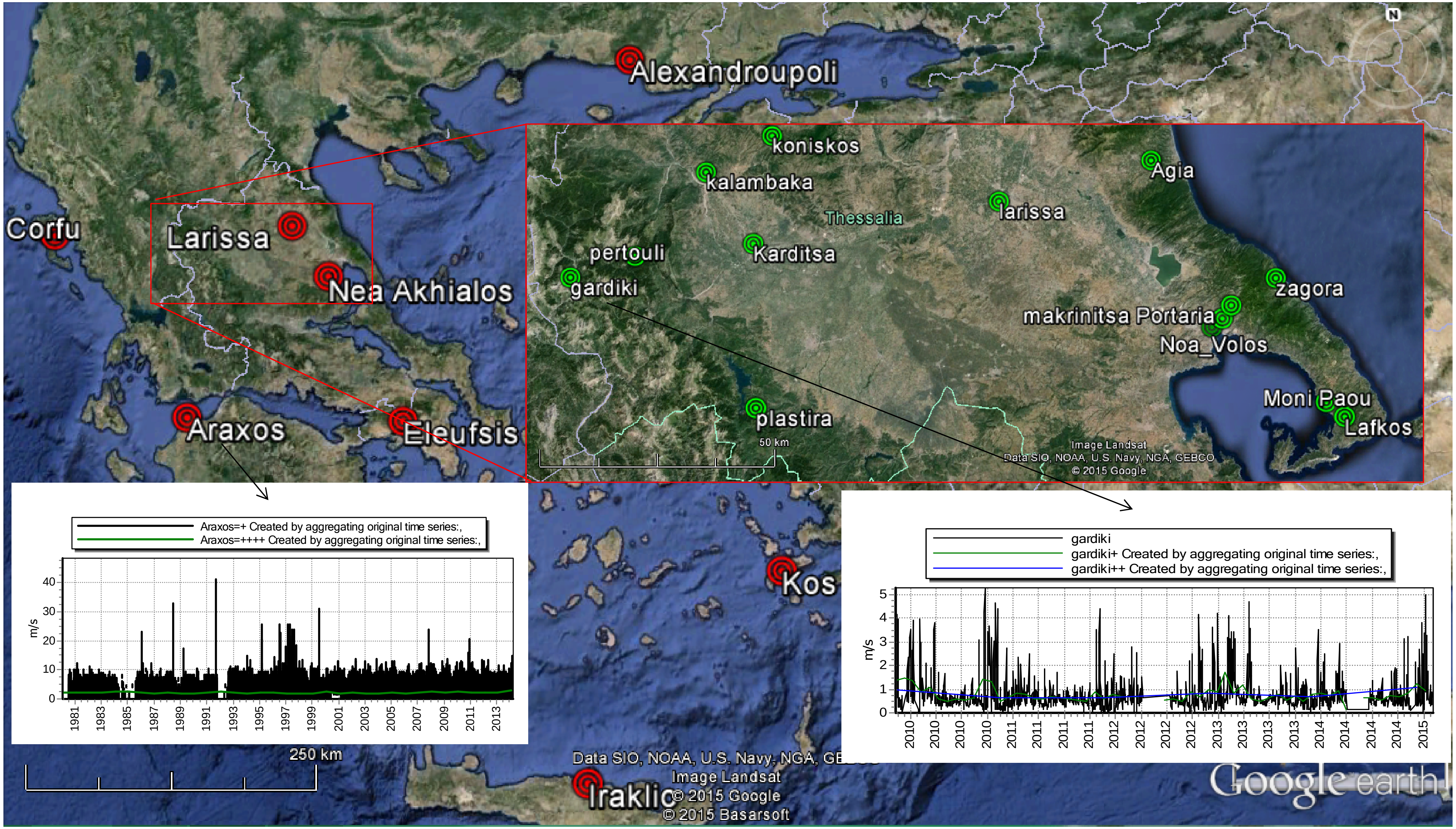


Figure 1: Locations of the meteorological stations at the area of interest (green-coloured) and at the wider area of Greece (red-coloured).

3. Marginal characteristics

To test the wind potential over the AoI (cf. [1]), we choose to analyze 16 stations from NOA (meteo.gr). Due to the minimum daily scale and the small number of years with available data, we also analyze 8 stations from allover Greece from HNMS (noaa.gov), which are in an hourly scale and include up to 75 years of measurements.

Table 1: General characteristics of stations over the AoI and allover Greece for wind speed and gust.

station name	source	longitude	latitude	elevation	no. years	mean wind speed (m/s)	std wind speed (m/s)	skew wind speed (m/s)	mean gust speed (m/s)
Alexandroupoli	HNMS	25.917	40.850	3.0	75	3.629	3.147	0.997	15.216
Araxos	HNMS	21.417	38.150	12.0	60	2.607	2.105	0.611	12.475
Eleufsis	HNMS	23.550	38.067	31.0	49	3.065	2.349	1.070	12.384
Iraκlio	HNMS	25.183	35.333	39.0	75	4.583	2.918	0.752	12.678
Corfu	HNMS	19.917	39.617	4.0	75	2.174	3.166	0.805	16.460
Kos	HNMS	27.067	36.783	129.0	34	4.844	2.619	1.279	13.211
Larissa	HNMS	22.417	39.633	74.0	74	1.669	2.709	0.327	14.728
Nea Akhialos	HNMS	22.800	39.217	15.0	37	3.258	2.331	1.501	12.780
agia	NOA	22.80	39.70	172.0	4	1.171	0.566	1.175	9.929
volos	NOA	22.96	39.38	54.5	9	1.007	0.801	2.397	9.857
uth volos	NOA	21.30	39.50	11.5	2	1.277	1.087	1.494	11.057
gardiki	NOA	22.93	39.36	1110.0	6	0.784	0.716	2.738	9.073
zagora	NOA	23.10	39.50	510.0	7	0.849	0.808	2.503	10.154
kalampaka	NOA	21.63	39.71	245.0	3	1.059	0.537	0.775	9.014
karditsa	NOA	21.90	39.40	96.0	2	1.097	0.791	1.525	7.282
koniskos	NOA	21.80	39.78	834.0	6	1.100	0.790	1.812	10.204
larissa	NOA	22.40	39.63	90.0	6	0.352	0.373	3.180	6.333
lafkos	NOA	23.25	39.18	334.0	4	1.339	0.867	1.532	10.133
plastira	NOA	21.79	39.24	865.0	6	2.728	2.175	2.384	13.005
makrinitsa	NOA	22.98	39.40	855.0	7	2.788	1.800	1.619	14.078
moni paou	NOA	23.20	39.21	152.0	2	2.106	1.675	1.280	12.035
pertouli	NOA	21.46	39.54	1175.0	8	0.866	0.733	2.438	9.664
portaria	NOA	22.92	39.20	603.0	3	1.651	1.260	1.667	12.262
trikala	NOA	21.76	39.56	168.0	9	0.800	0.531	1.886	8.546

4. Cyclostationarity

The wind process (like any other hydrometeorological process) includes two cyclostationarities, one seasonal and one daily (cf. [2]). We apply a simple model of double periodicity (described by the equations below) to catch simultaneously both of them using nine dimensionless coefficients:

$$\mu_c(t) = A(t)e^{-\cos(2\pi(t+B(t))/24)} + C(t)/\mu_h \quad (1)$$

$$A(t) = a_A \cos\left(2\pi\frac{(t+b_A)}{12*24*30.5}\right) + c_A/\mu_h \quad (2)$$

$$B(t) = a_B \cos\left(2\pi\frac{(t+b_B)}{12*24*30.5}\right) + c_B/\mu_h \quad (3)$$

$$C(t) = a_C \cos\left(2\pi\frac{(t+b_C)}{12*24*30.5}\right) + c_C/\mu_h \quad (4)$$

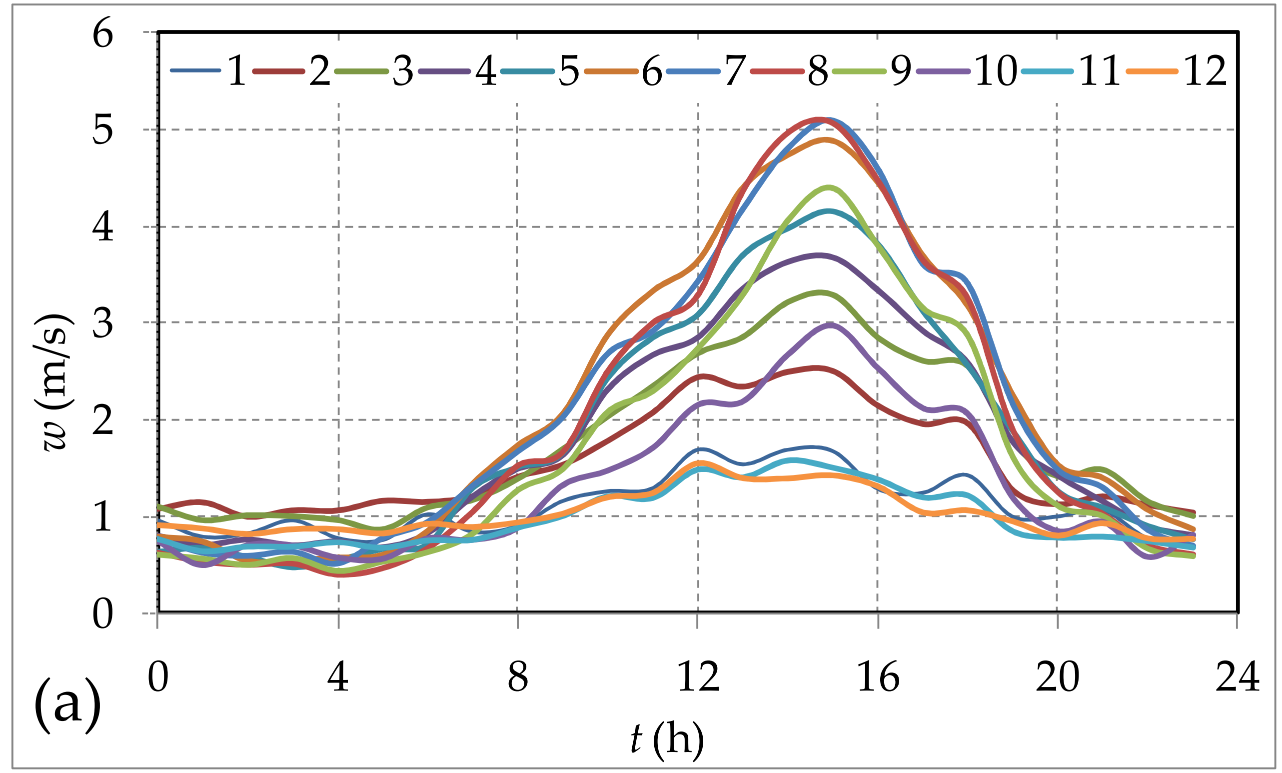
Table 2: Model coefficients for the Larissa station (HNMS).

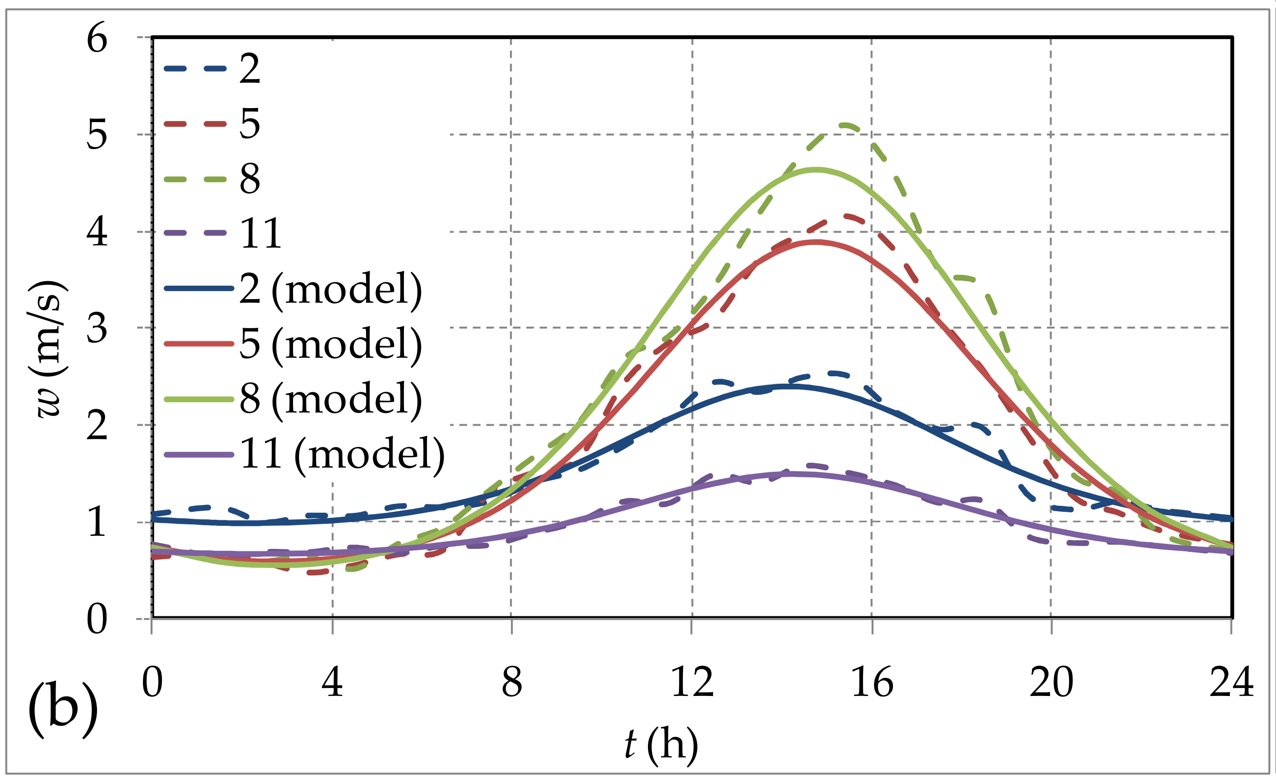
	A	B	C
a	0.463	0.736	-0.144
b	-1.107	-6.558	-6.776
c	0.323	1.039	-1.619

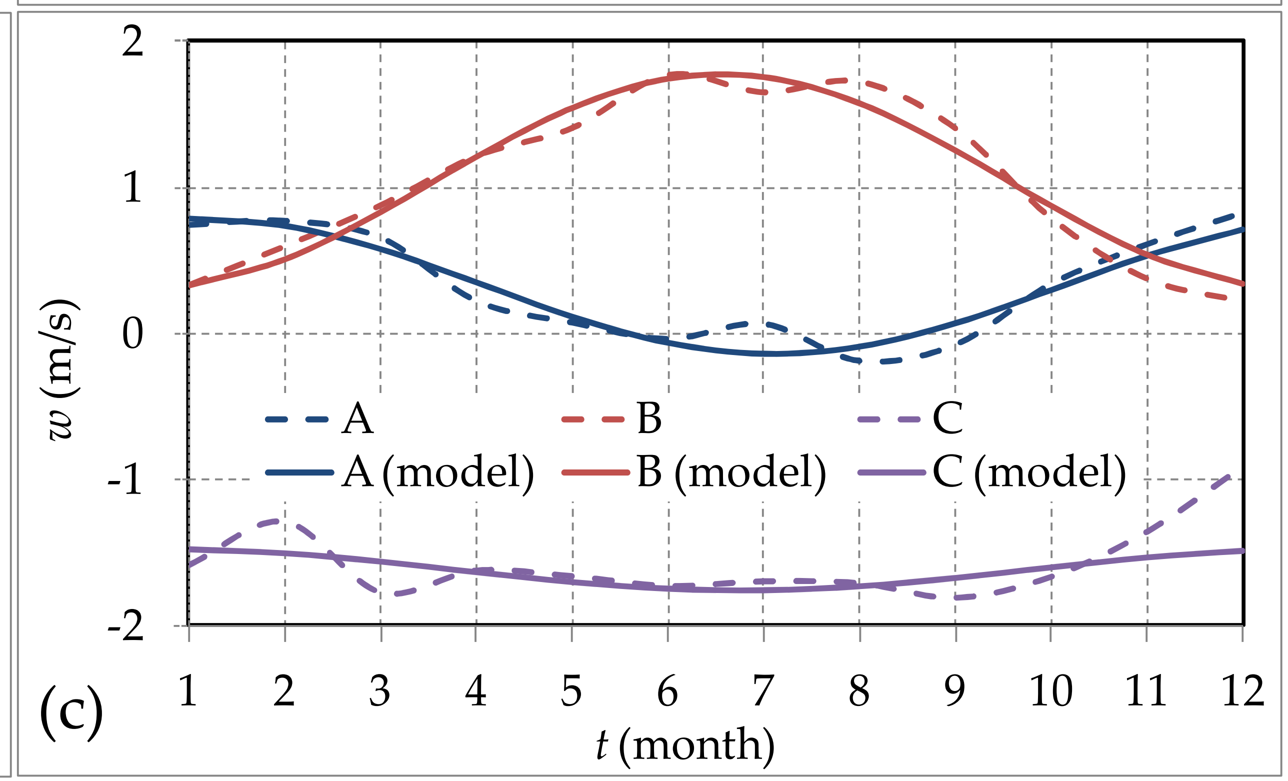
where t denotes time in hours; a_A, a_B, a_C are dimensionless coefficients; b_A, b_B, b_C are in time units; c_A, c_B and c_C are in m/s; andμ_h is the hourly mean of the process.

5. Cyclostationarity (cont.)

Figure 2: (a) within-day fluctuation of hourly mean wind speed (*w*) for each month; (b) cyclostationary model fitting for months 2 (Feb.), 5 (May), 8 (Aug.) and 11 (Nov.); and (c) monthly fluctuation of cyclostationary model coefficients. All correspond to the Larissa station (HNMS).







6. Probability functions

For the marginal distribution functions of *w*, we check the Normal, Gamma and Weibull (cf. [3]), using maximum likelihood algorithms for the parameters' estimation (neglecting the low *w* part). For the Larissa station the minimum error corresponds to the Gamma function (with k=4.829 and θ=0.758), while for most other stations is the Normal one.

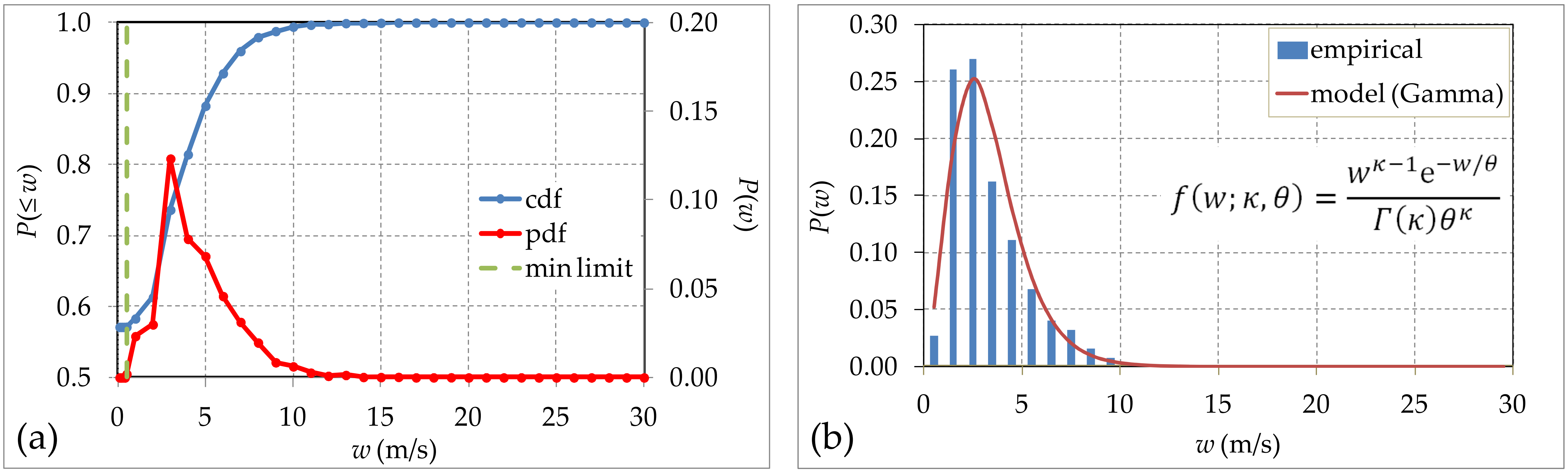


Figure 3: (a) Empirical cumulative and probability density functions of wind speed (with low value limit); and (b) fitting of the Gamma function for the Larissa station.

7. Probability function (cont.)

For the marginal distribution functions of wind gust (w_g), we check the General Extreme Value (GEV), Burr and Generalized Gamma (cf. [4]), using again the method of maximum likelihood. For the Larissa station the minimum error corresponds to the Burr function (with a=12.125, c=9.865 and l=0.831), while for most other stations is the GEV one.

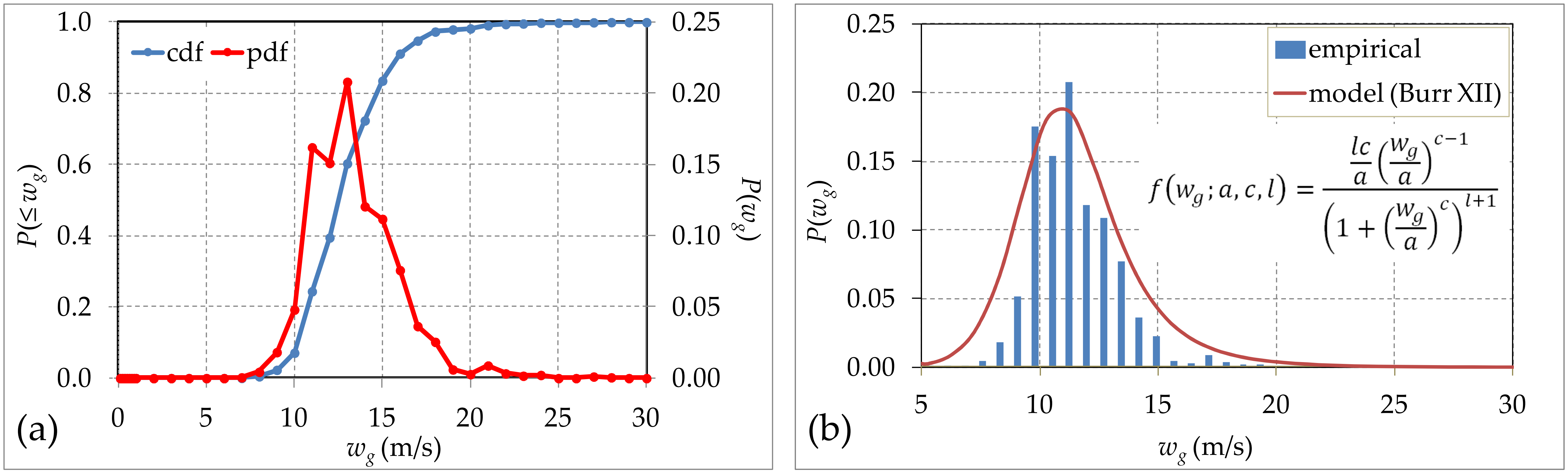


Figure 4: (a) Empirical cumulative and probability density functions of wind gust; and (b) fitting of the Burr function for the Larissa station.

8. Stochastic structure

We investigate the structure of the wind process with the climacogram (i.e. variance of the averaged process versus averaging time scale). This choice is based on the analysis of [5], where the aforementioned stochastic tool resulted (for all the examined processes, e.g. Markov, HK and combinations thereof) in a smaller statistical uncertainty (i.e. mean-squared error) for the majority of scales, in comparison to the power spectrum and autocovariance. In the equations below, we show its definition and expected value of its classical estimator:

$$\gamma(m) := \operatorname{Var}\left[\int_0^m \underline{w}(\xi)\mathrm{d}\xi\right]/m^2 \quad (5)$$

$$\mathrm{E}\left[\underline{\hat{\gamma}}(k\Delta)\right] = \frac{1-\gamma(n\Delta)/\gamma(k\Delta)}{1-k/n}\gamma(k\Delta) \quad (6)$$

where the underlined symbols denote random variables, *m* (in units of time) and *k* (dimensionless) are the scales of the continuous and discrete-time process, *Δ* is the sampling time interval and *n* is the total number of observations.

9. Stochastic structure (cont.)

We estimate the empirical climacogram (from hourly to climatic scale) for the long timeseries of NOA and then, we fit an HK model to the apparent long-term behaviour:

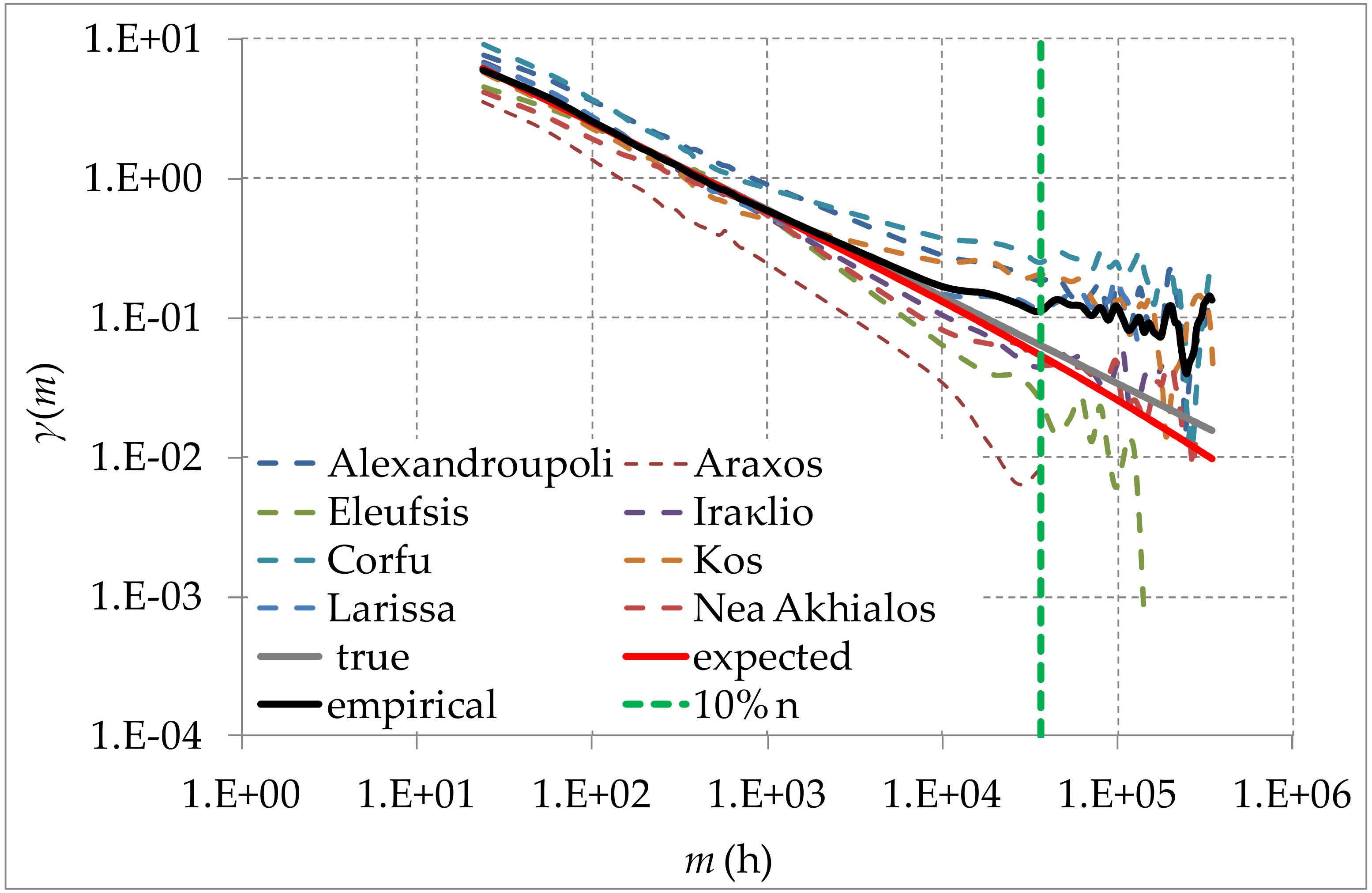


Figure 5: Larissa, Note that we fit the model up to 10% of n (following the rule of thumb, cf. [5]).

$$\gamma(m) = \frac{\lambda}{m^{2-2H}} \qquad (7)$$

We calculate that the best fit, for scales up to 10% n, is for $\lambda \approx 45$ m^2/s^2 and $H \approx 0.7$ (Hurst coefficient, ranging from 0 to 1), with correlation coefficient of $R^2 \approx 95\%$ (note that the empirical variance's deviation from the power-law model at latter scales, is characterized by high uncertainty).

10. Stochastic generation of hourly wind speed

For the wind turbines installation we choose the area near the Plastira station, which exhibits the larger hourly mean wind speed, i.e. 11.782 m/s (calculated by multiplying the daily mean with 4.458, which is the ratio of the mean values of the HNMS and NOA stations of Larissa).

We can then produce an hourly wind speed timeseries by preserving the cyclostationary-deterministic model of Larissa station (which is the nearest one with a long period and an hourly time-step), the desired distribution function and the HK stochastic process (following [5]).

We finally categorize the wind turbine generator into class II, based on the IEC-61400 standards (cf. [6]) and for an annual average wind speed greater than 10 m/s as well as for a reference one approx. 33 m/s (estimated from the wind gust distribution function of the Larissa station). A possible industrial solution for the wind turbine is the ENERCON E-82 (e.g. [1]).

11. Energy production forecasting

Furthermore, we can estimate the hourly energy production (denoted E) based on the turbine's power curve (a time-window of the first month of the simulation is shown below).

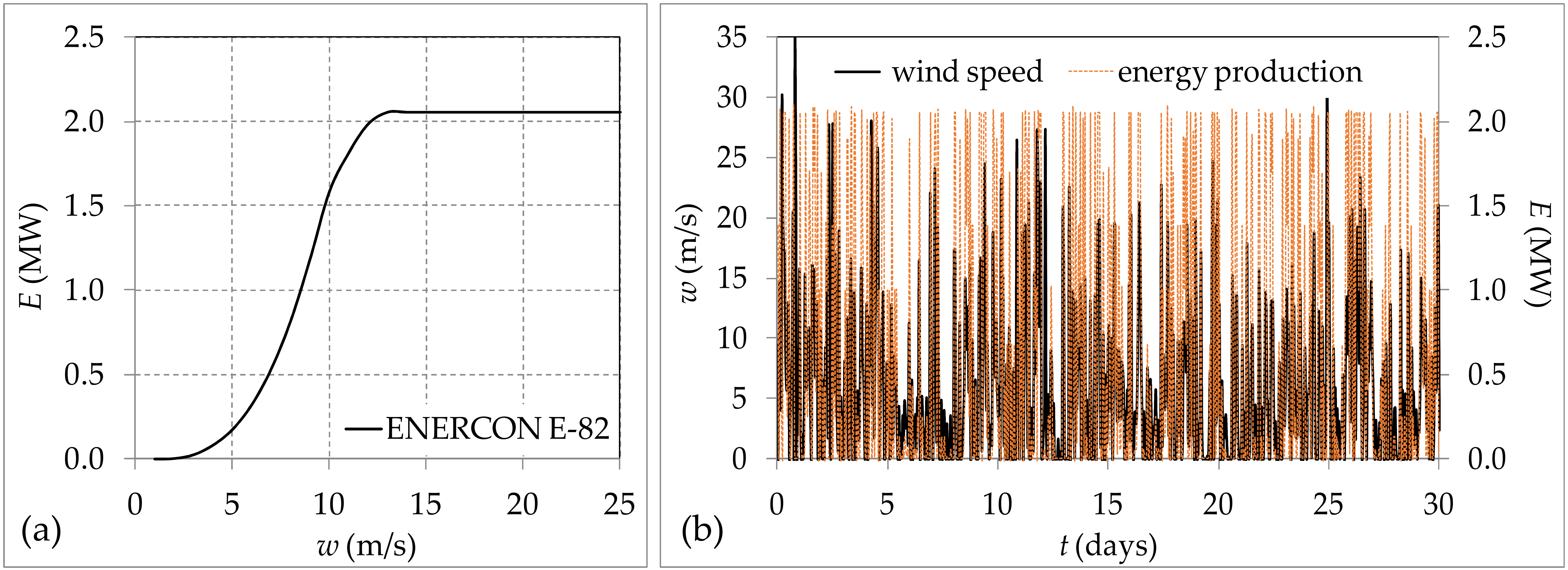


Figure 6: (a) wind turbine power curve (enercon.de) and (b) one month wind speed forecasting and the corresponding energy production from the wind turbine.

12. Conclusions

We present a methodology for constructing a wind process and energy production model on an hourly time-scale, essential for the energy management of renewable sources. This model can preserve both daily and seasonal periodicity as well as the distribution function and stochastic structure of the process. Additionally, we apply the model to the area of Thessaly (Greece) and we propose an industrial wind-turbine solution based on the IEC-61400 standards classification.

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References

1) Pappa, I., Y. Dimakos, P. Dimas, P. Kossieris, P. Dimitriadis, and D. Koutsoyiannis, Spatial and temporal variability of wind speed and energy over Greece, *European Geosciences Union General Assembly 2014*, Geophysical Research Abstracts, Vol. 16, Vienna, EGU2014-13591, European Geosciences Union, 2014.
2) Belu, R., and D. Koracin, Statistical and spectral analysis of wind characteristics relevant to wind energy assessment using Tower Measurements in Complex Terrain, *Journal of Wind Energy*, p. 1-12, 2013.
3) Waewsak, J., C. Chancham, M. Landry and Y. Gagnon, An analysis of wind Speed distribution at Thasala, Nakhon Si Thammarat, Thailand, *Journal of Sustainable Energy and Environment*, 2, 51-55, 2011.
4) Chiodo, E., D. Lauria and C. Pisani, Bayes estimation of wind speed extreme values, *Renewable Power Generation Conference* (RPG 2014), Naples, 2014.
5) Dimitriadis, P., and D. Koutsoyiannis, Climacogram versus autocovariance and power spectrum in stochastic modelling for Markovian and Hurst–Kolmogorov processes, *Stochastic Environmental Research & Risk Assessment*, 2015.
6) Burton T., Sharpe D., Jenkins N. and Bossanyi E., Wind Energy Handbook, John Wiley & Sons, *New York*, 2001.