

Department of Civil and Environmental Engineering
Massachusetts Institute of Technology

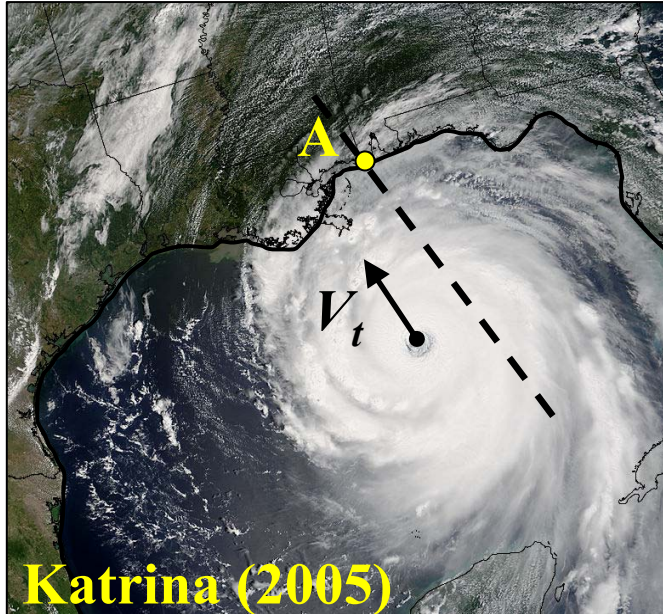
*Extreme Rainfall Intensities and
Long-term Rainfall Risk from
Tropical Cyclones*

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Objective

Long-term rainfall risk from TCs at location A:



$\lambda_D(i)$: rate at which $I_{max}(D)$ exceeds i at location A (events/year)

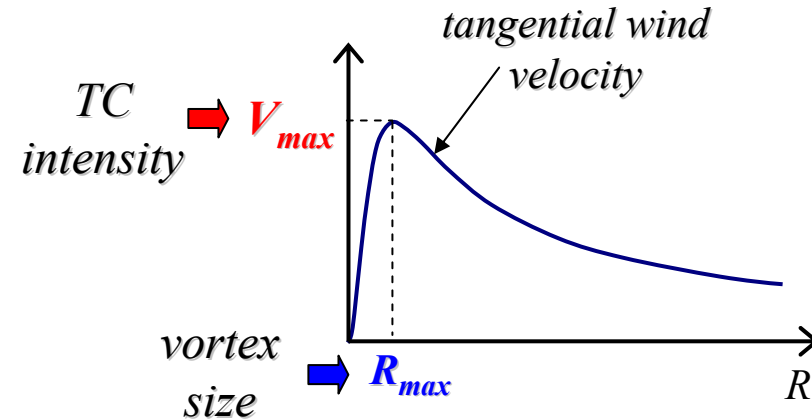
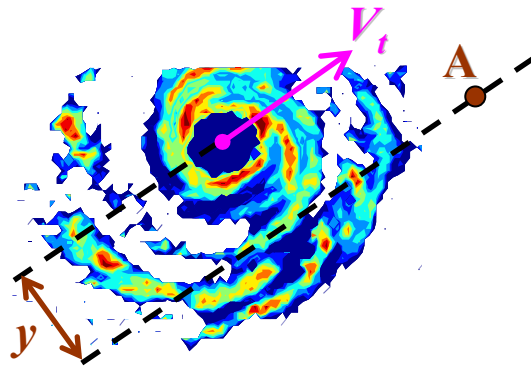
$I_{max}(D)$: maximum rainfall intensity at location A for averaging duration D

Risk analysis \Rightarrow $\lambda_D(i) = \lambda \int_{\text{all } \omega} P[I_{max}(D) > i | \omega] P[\omega] d\omega$

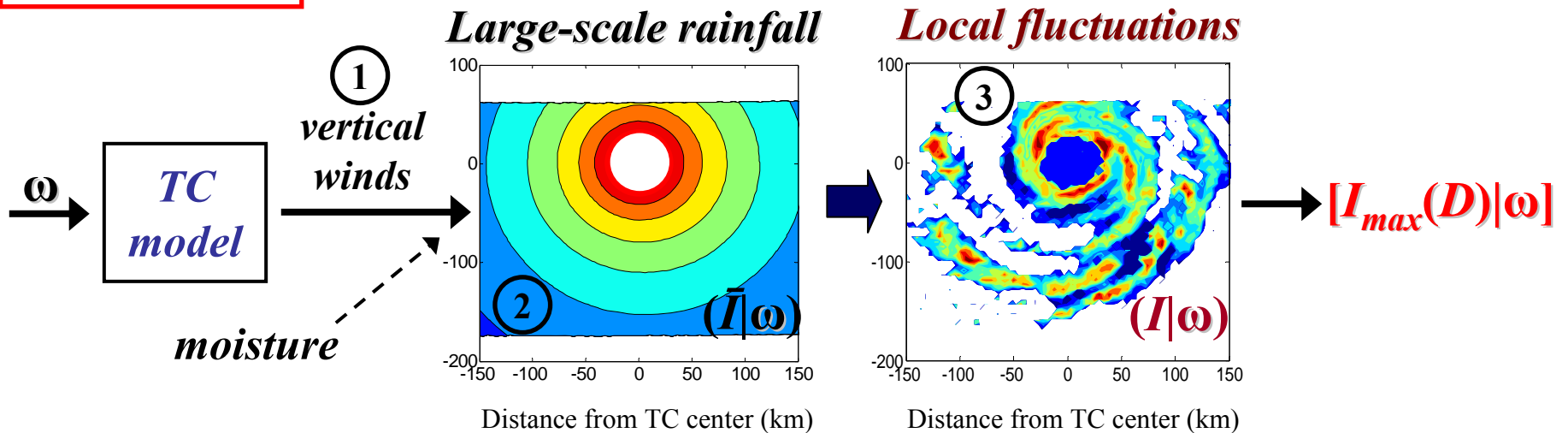
λ (TC arrival rate [events/yr]) is labeled as **focus**.
 $P[\omega]$ is labeled as *local recurrence (literature)* and *TC characteristics*.

Implementation

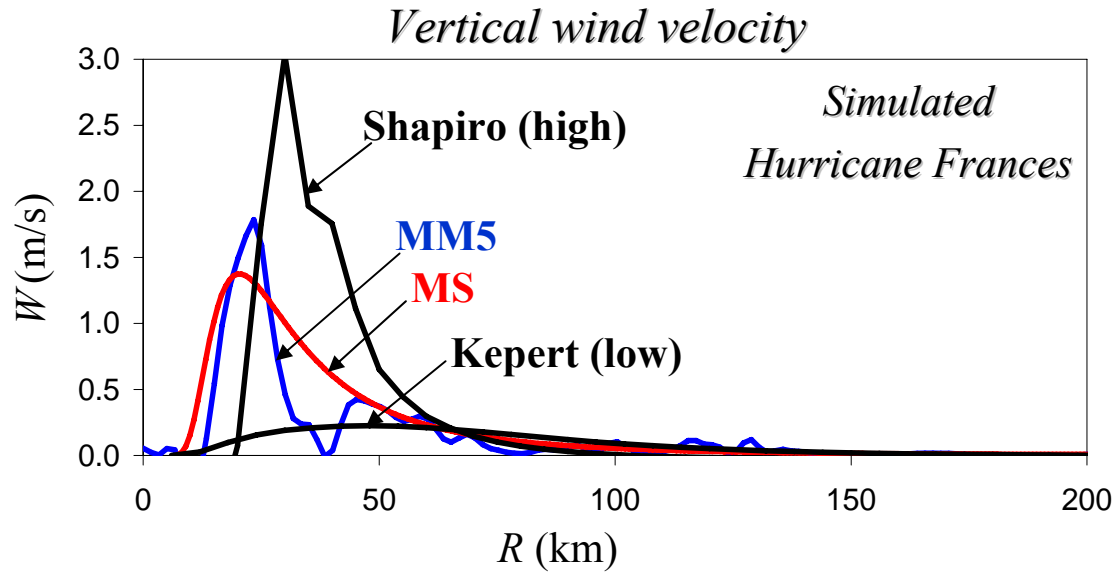
➤ parameters $\omega = [V_{max}, R_{max}, V_t, y]$



$[I_{max}(D)|\omega]$



TC Model: Vertical winds and Rain



Vertical winds

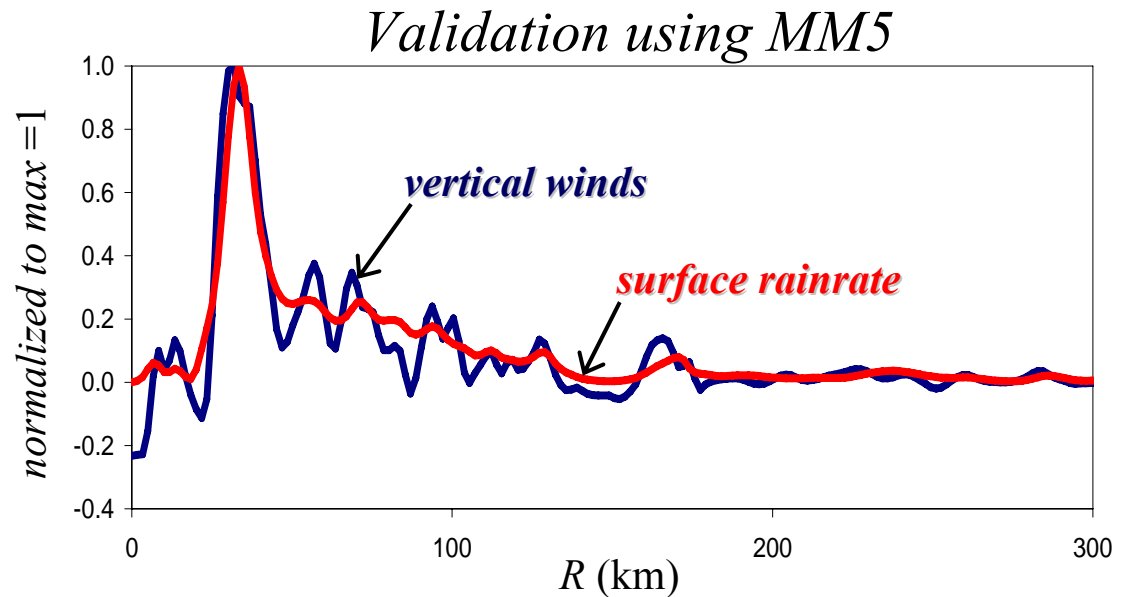
Rain:

$$\bar{I} = c W$$

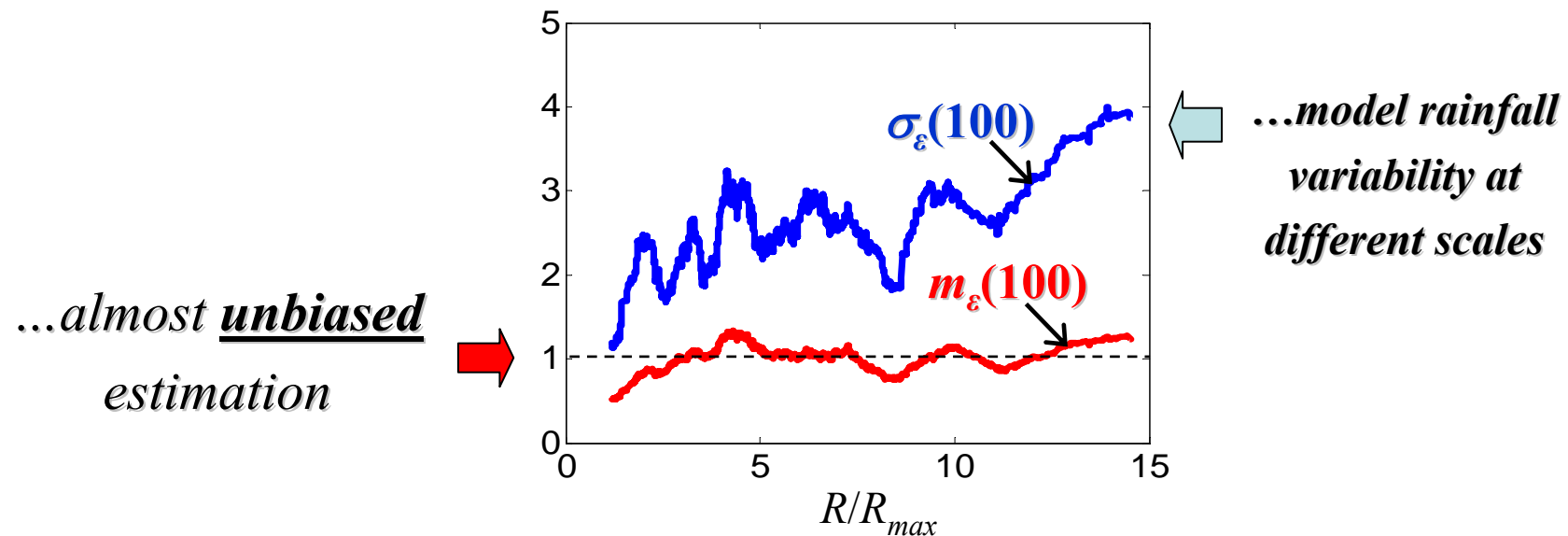
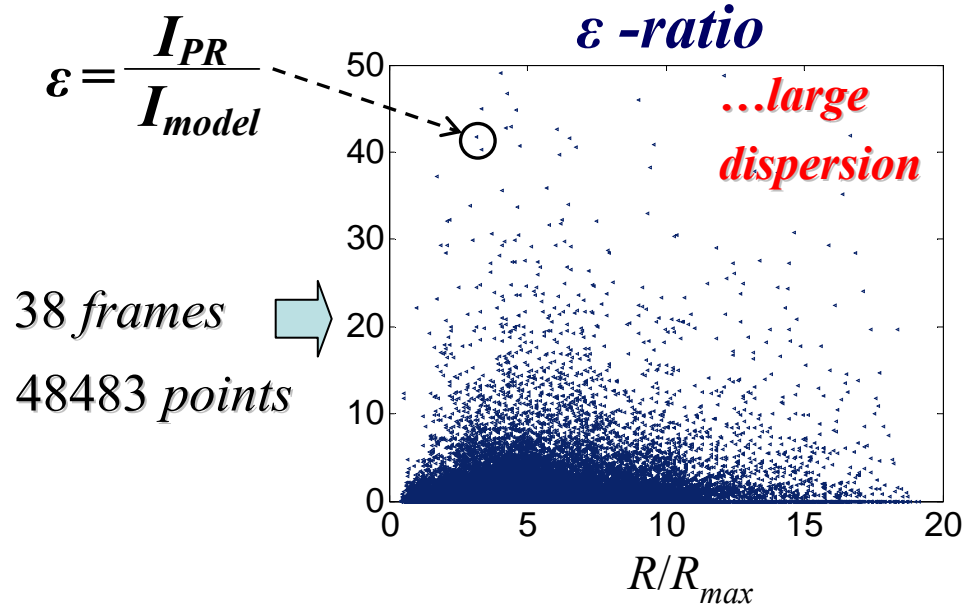
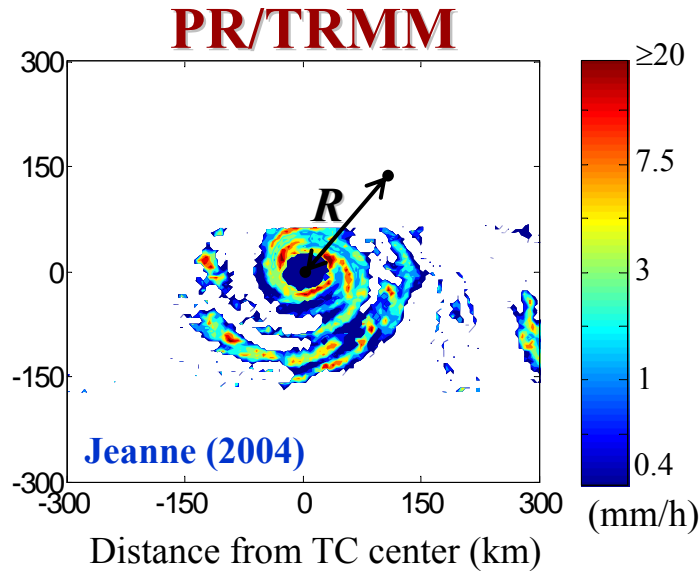
rainrate

moisture content of air

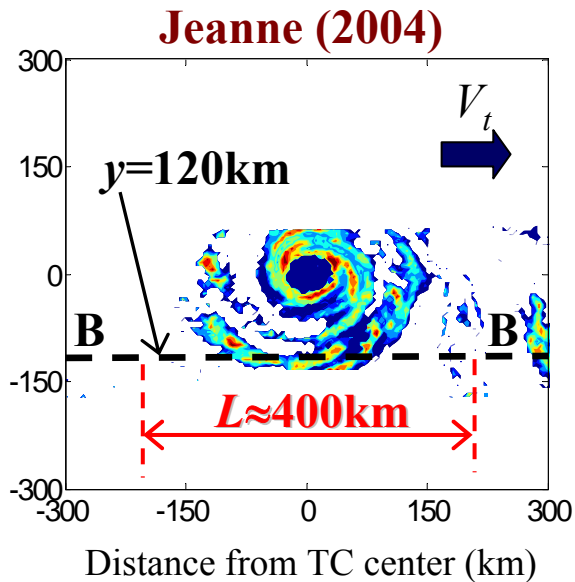
vertical wind speed



Validation using PR/TRMM data

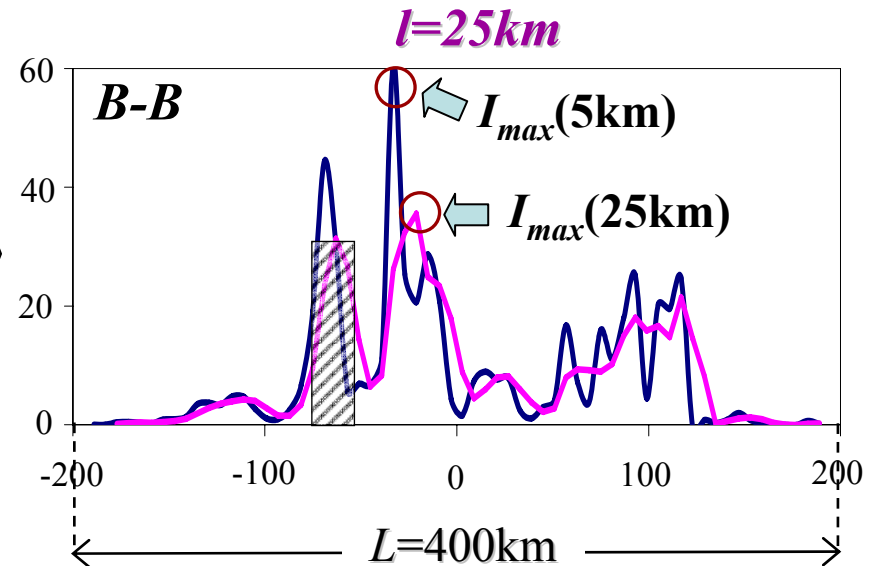
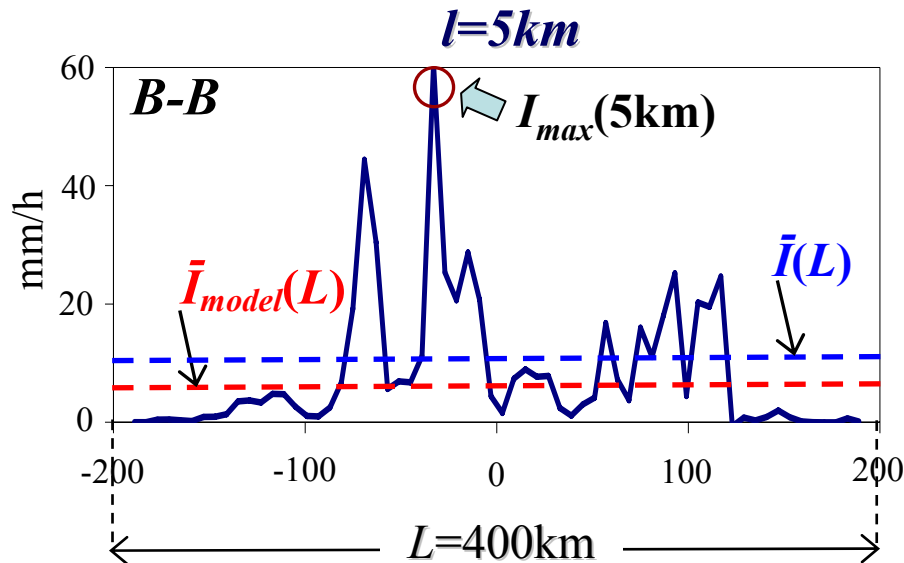


Statistical model of $[I_{max}(L)|\omega]$



$$I_{max}(L) = \overbrace{\bar{I}_{model}(L)}^{(large-scales)} \beta \underbrace{\gamma_{max}(L)}^{(small-scales)}$$

model estimate for the mean rainfall intensity inside L (points to $\bar{I}_{model}(L)$)
corrects the model mean relative to the empirical mean (points to β)
amplification factor for the maximum inside l (points to $\gamma_{max}(L)$)



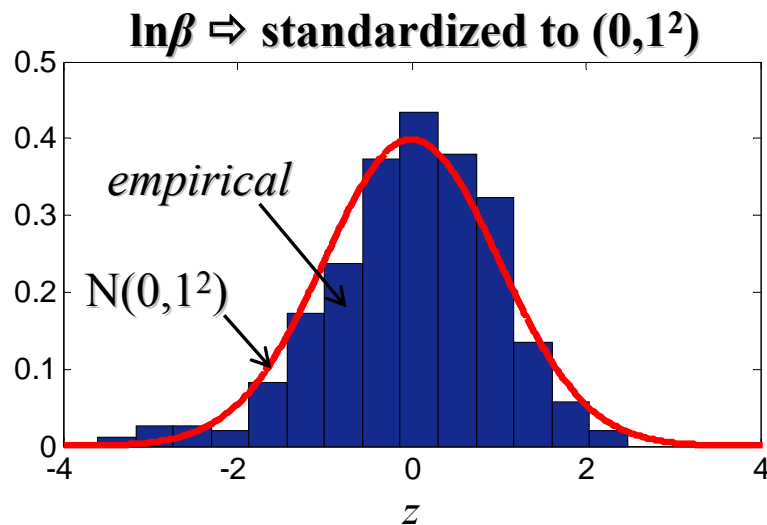
Statistical models for $[\beta|\omega]$ and $[\gamma_{max}(l)|\omega]$

Model for $[\beta|\omega]$

$$\beta = \frac{\bar{I}(L)}{\bar{I}_{model}(L)}$$

$\bar{I}(L)$ → empirical
 $\bar{I}_{model}(L)$ mean inside L
 ↓
 model estimate

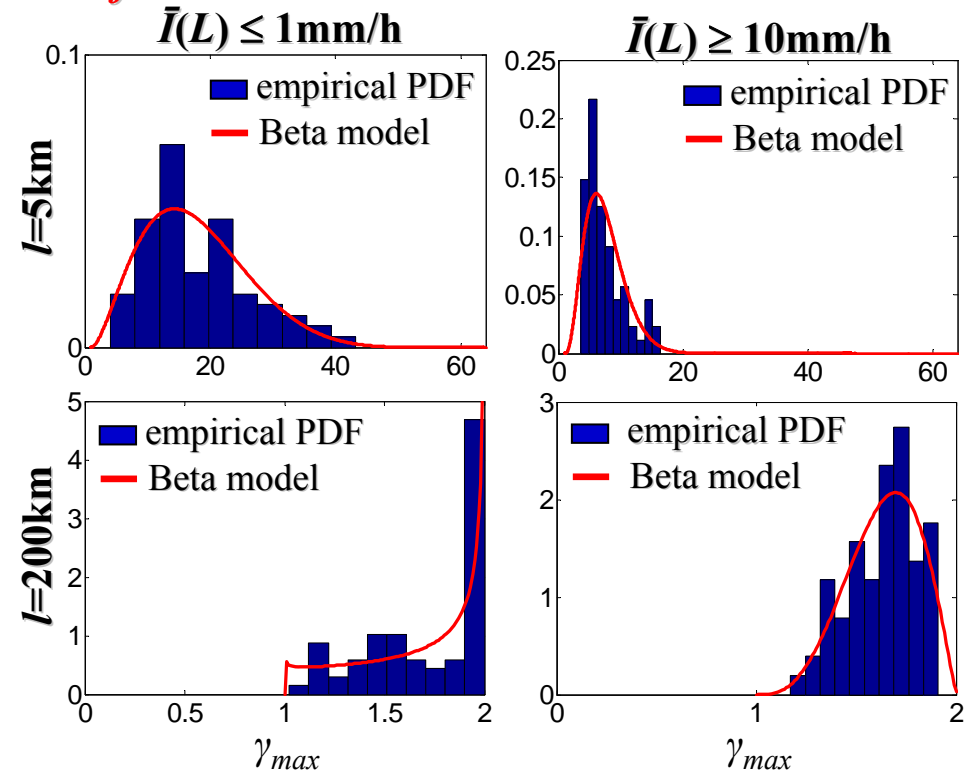
... $\beta(y, \bar{I}_{model}) \sim \text{lognormal}$



Model for $[\gamma_{max}(l)|\omega]$

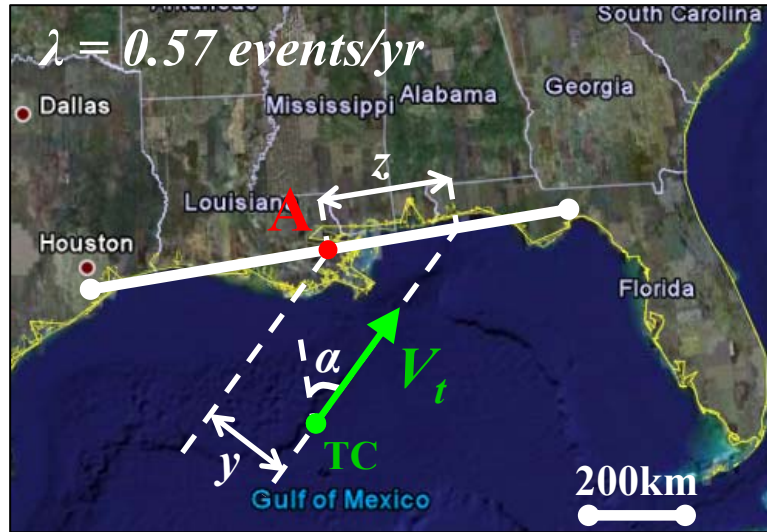
$$\gamma_{max}(l) = \frac{I_{max}(l)}{\bar{I}(L)}$$

$I_{max}(l)$ → maximum rainfall intensity at scale l
 $\bar{I}(L)$ mean inside L
 ↓
 parameterize in terms of \bar{I}



Application to New Orleans

➤ Recurrence model for $\omega = [V_{max}, R_{max}, V_t, y]$



$$[V_{max} | \Delta P] \sim \left\{ \begin{array}{l} \text{lognormal with} \\ m = 4.8 \Delta P^{0.559}, \sigma = 0.15 \text{ m} \\ \text{(Willoughby and Rahn, 2004)} \end{array} \right\} \quad \text{(ind.)}$$

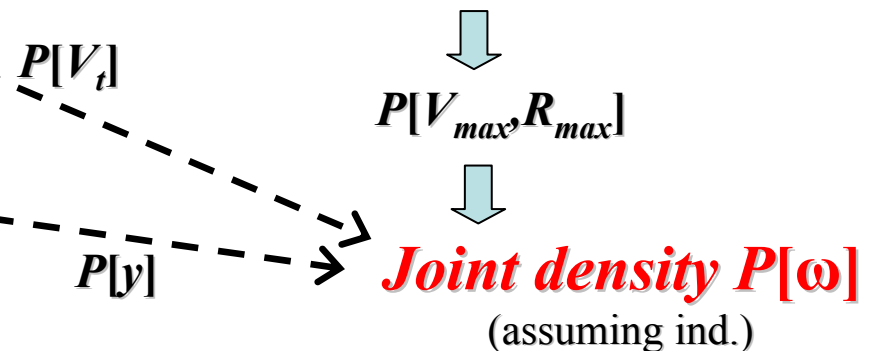
$$[R_{max} | \Delta P] \sim \left\{ \begin{array}{l} \text{lognormal with} \\ m = 3.962 - 0.00567 \Delta P, \sigma = 0.313 \\ \text{(Vickery et al., 2000)} \end{array} \right\}$$

$$\Delta P(\text{mb}) \sim \left\{ \begin{array}{l} \text{shifted lognormal with} \\ m_{\ln \Delta P} = 3.15, \sigma_{\ln \Delta P} = 0.68, \\ \text{Shift par.} = 18\text{mb (IPET, 2006)} \end{array} \right\}$$

$$V_t \sim \left\{ \begin{array}{l} \text{LN with } m = 6\text{m/s} \text{ \& } \sigma = 2.5\text{m/s} \\ \text{(Vickery et al., 2000, Chen et al. 2006)} \end{array} \right\}$$

$$\left. \begin{array}{l} z \sim \text{U}[-500\text{km}, 500\text{km}] \\ \alpha \sim \text{N}[-5.4^\circ, (34.9^\circ)^2] \\ \text{(IPET, 2006)} \end{array} \right\} \text{(ind.)} \Rightarrow$$

$$y = -z \cos(\alpha)$$

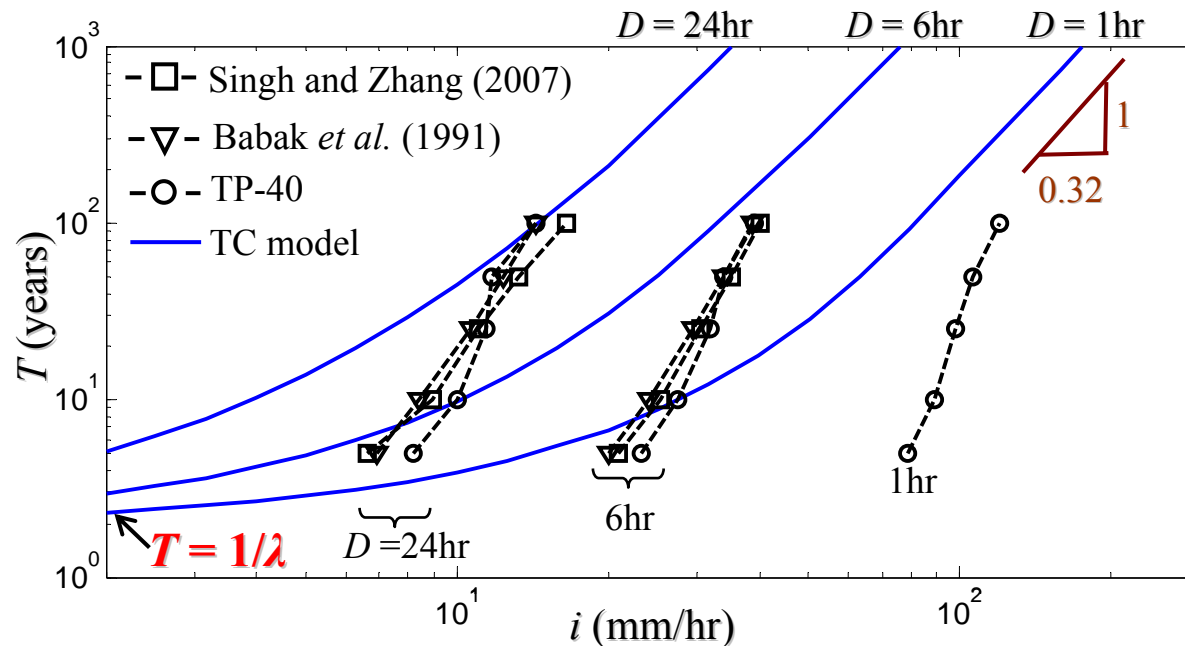
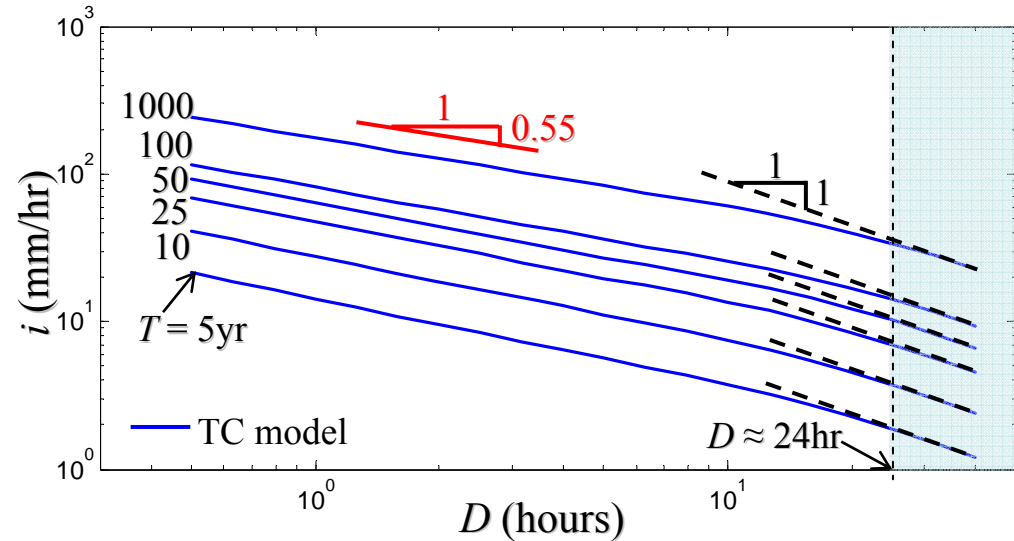


Application to New Orleans: IDF curves

Rainfall Risk and IDF curves:

$$\lambda_D(i) = \lambda \int_{\text{all } \omega} P[I_{\max}(D) > i | \omega] P[\omega] d\omega$$

IDFs: plots of i against D and $T = 1/\lambda_D(i)$ (years)



- For large D and T TCs dominate risk.
- For small D applies the rule: “convection is convection”

Conclusions

➤ We developed a *physical-statistical framework for peak TC rainfall intensities*

- $[I_{max}(D)|\omega]$ {
- *Explicit parameterization* of the hurricane: $\omega = [V_{max}, R_{max}, V_p, y]$
 - *Physical model* to obtain *large-scale rainfall* given ω
(inter-storm variability)
 - *Statistical model for rainfall fluctuations*
(intra-storm variability)

➤ *Model validation using PR/TRMM data*

➤ *Application to New Orleans* { *TCs dominate rainfall risk for*
 $D \geq 24h$ and $T \geq 100$ years

Future work {

- *effect of landfall and topography*
- *areal reduction* • *TC wind maxima*

Thanks!

