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# Stochastic investigation of temperature process for climatic variability identification

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The poster can be downloaded at: <http://www.itia.ntua.gr/>



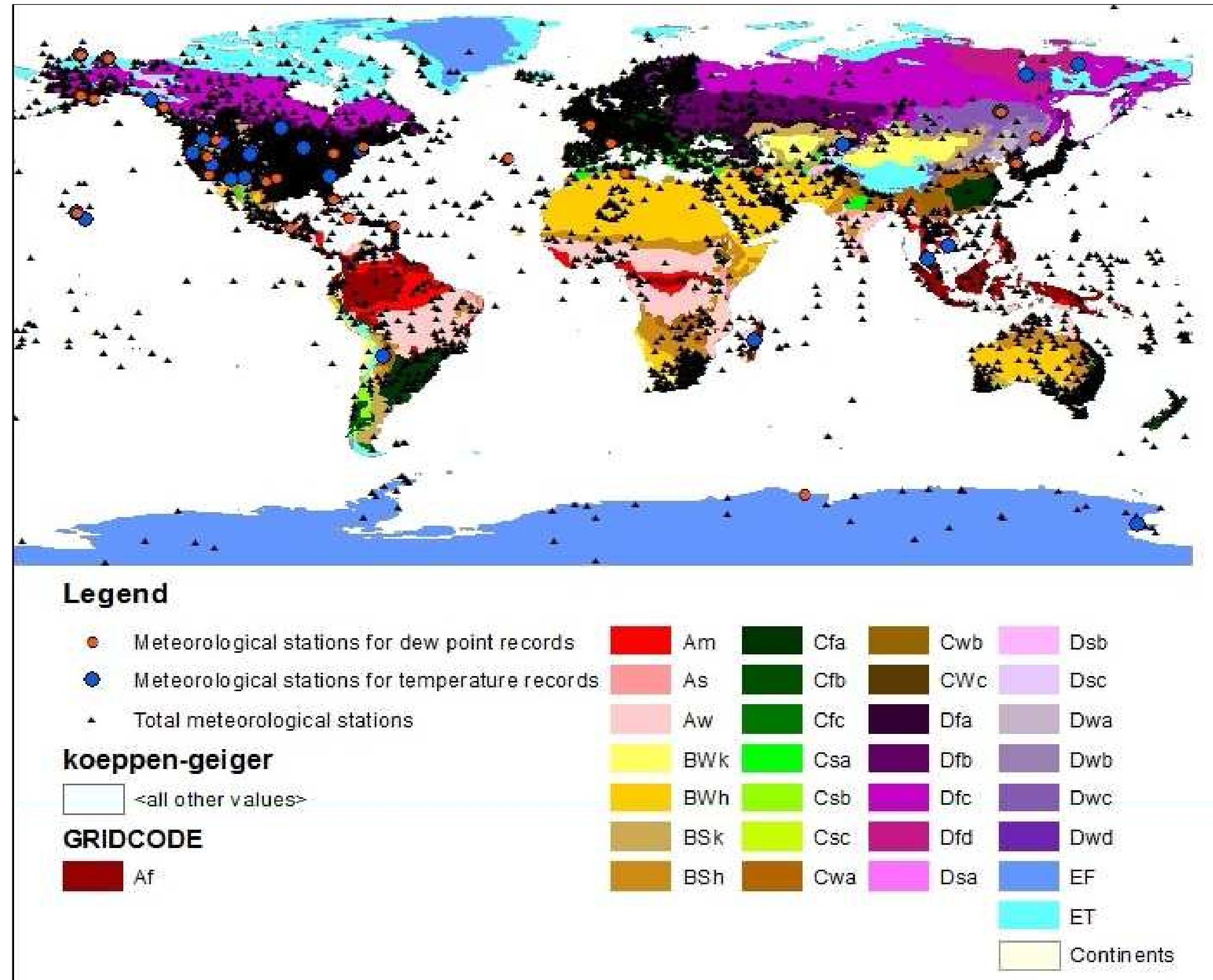


The purpose of this analysis is to examine the climatic variability of temperature and dew point time series using the Hurst- Kolmogorov model. A poly-parametric model of high-complexity such as the climatic dynamics, is now approached by a three-parameter Hurst- Kolmogorov stochastic model just in terms of evaluation of prediction interval.

The statistical uncertainty enclosed within the surface and dew temperature process is quantified through a Monte Carlo approach. The analysis is based on the assumptions that the ratio of the annual mean temperature divided by the annual standard deviation is a stationary process, normally distributed and that it follows one of the most commonly used stochastic models in geophysics, i.e., Markov and HK (including the White Noise process for  $H=0.5$ ). These assumptions are not only parsimonious, but also considered conservative, since any non-stationary approach would increase the complexity of the system and since the stochastic structure cannot be any less complex than the Markov and HK one-parameter models, which entail all exponential as well as a power-type behaviours. Furthermore, the analysis is applied for all climatic zones described in the Köppen system. Moreover, each mean annual value is considered valid when it is estimated from more than 1200 h, i.e. 4 measurements per day for at least 10 months. For the synthesis of the stochastic timeseries, we use the 3×AR(1) technique described in [4]:

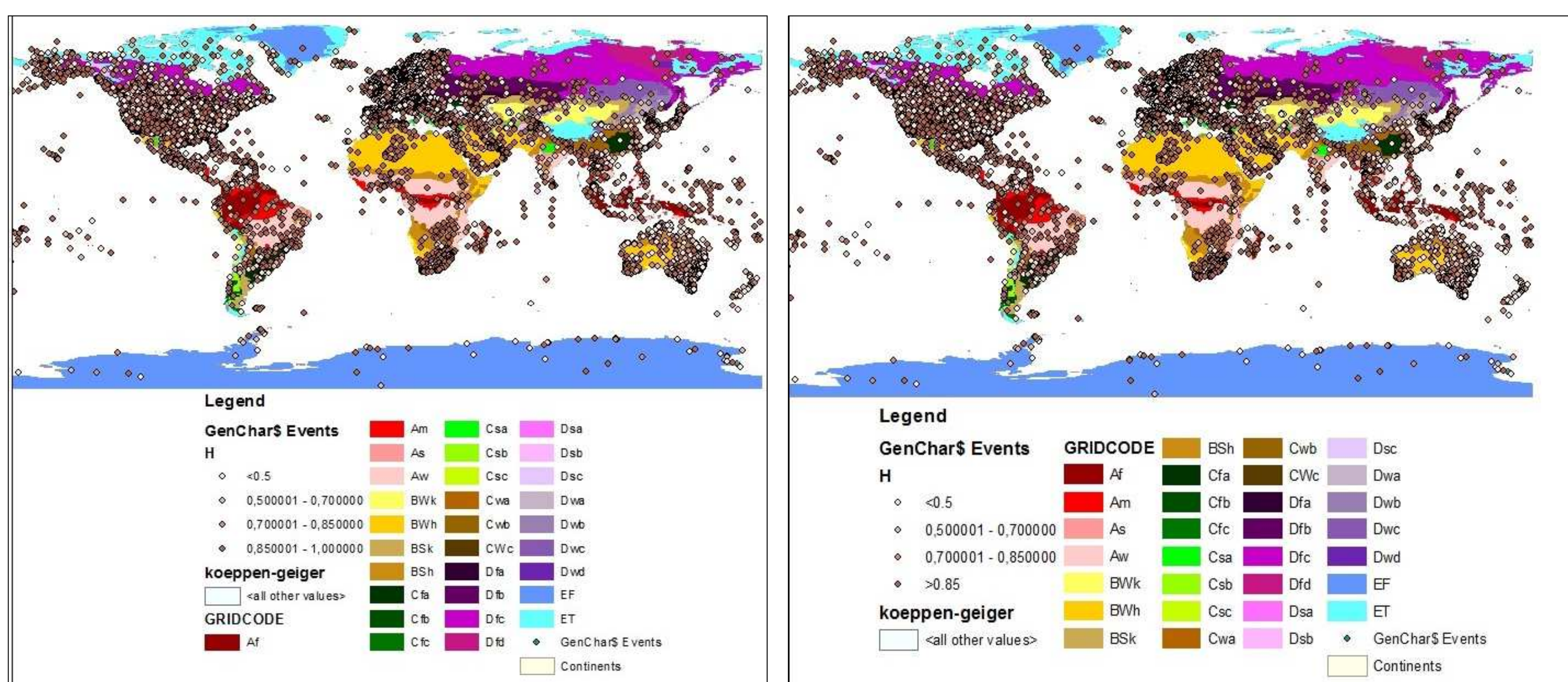
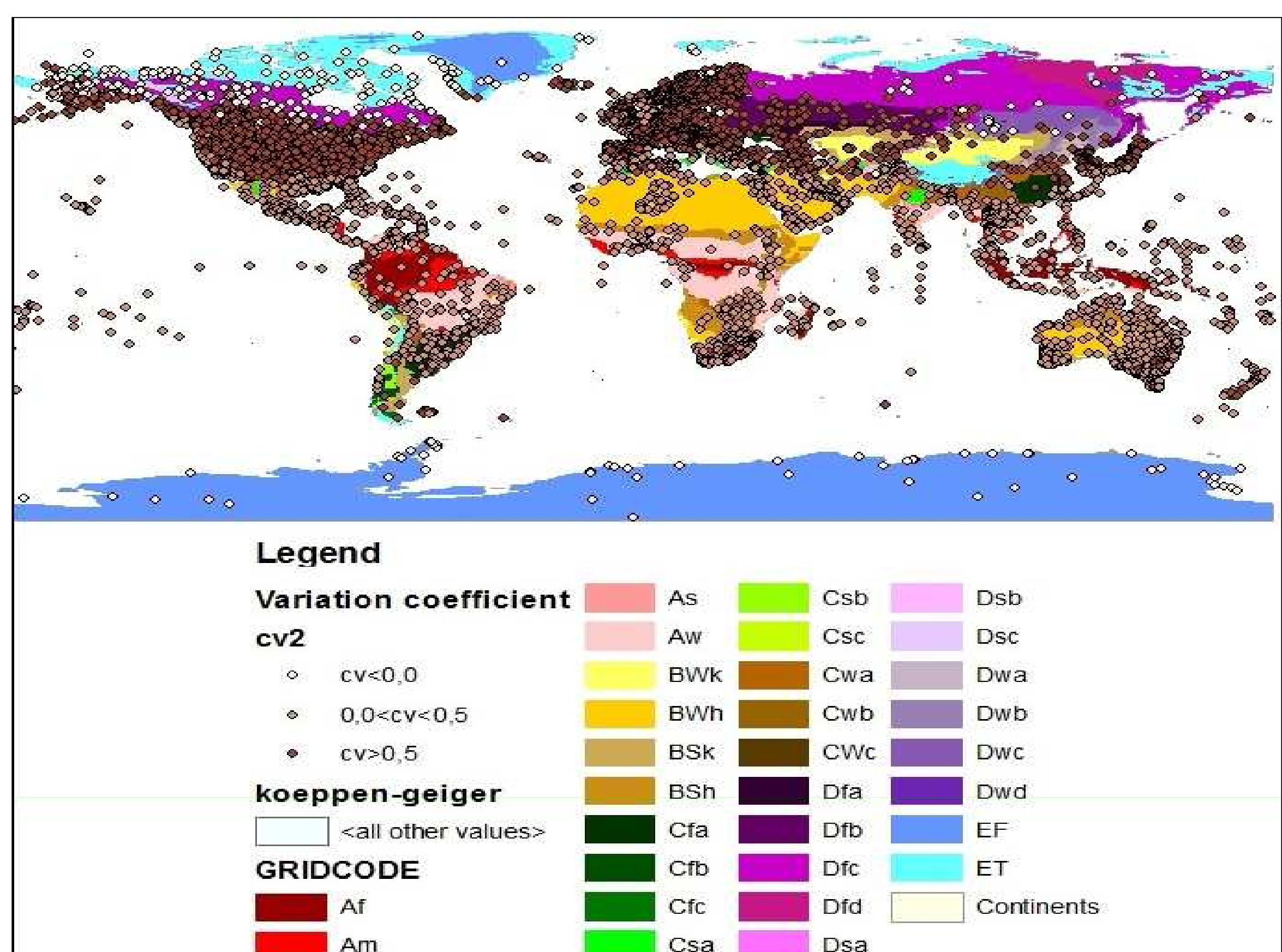
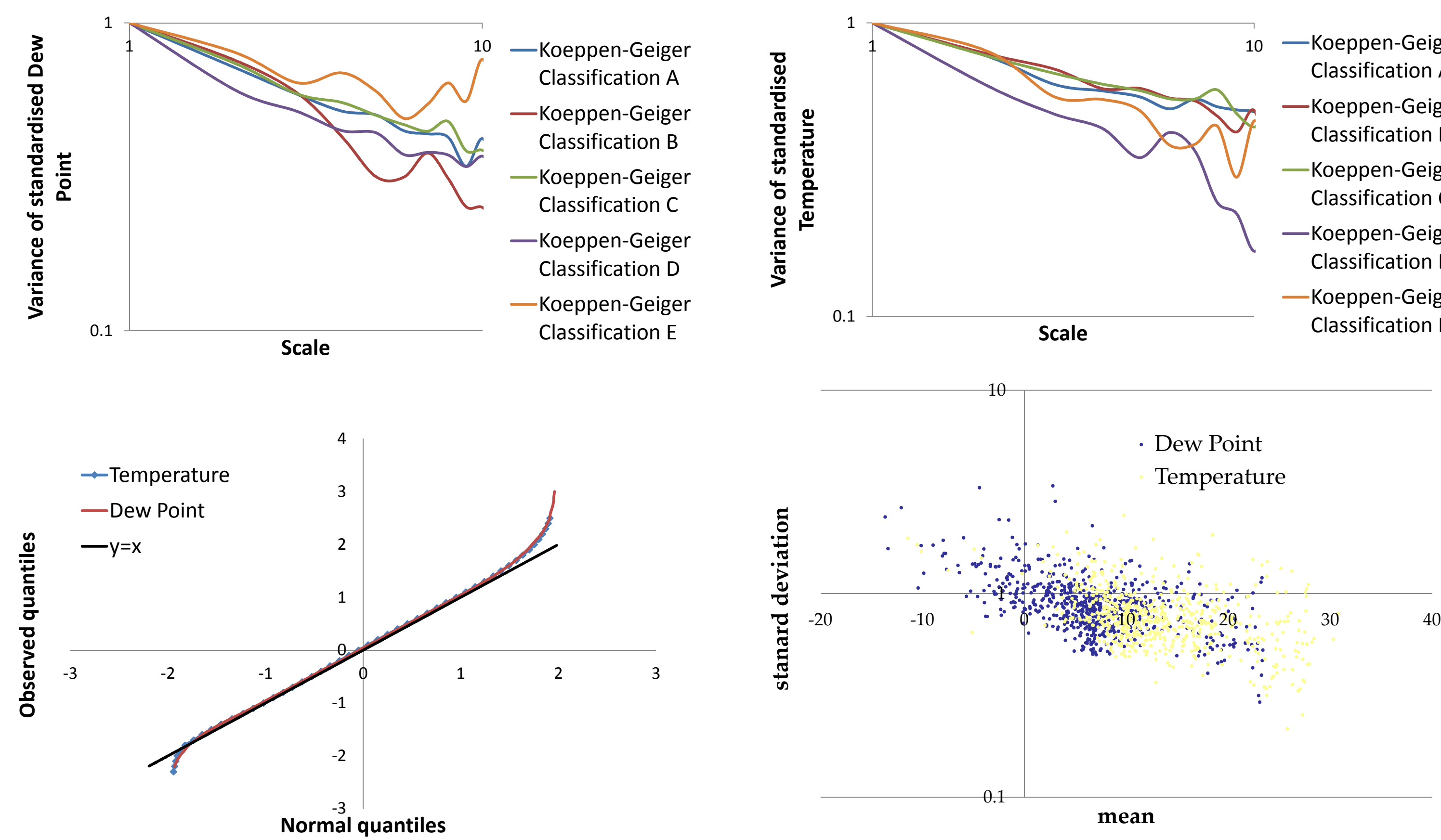
$Q, \Gamma(1) = 0.932 + 0.087 H, H \leq 0.76$ , or  $Q, \Gamma(1) = 0.993 + 0.007 H, H > 0.76$ , where  $H$  is the Hurst-Kolmogorov coefficient.

Based on the Monte Carlo results, we estimate the prediction interval of each 30-year mean, standard deviation, minimum and maximum values. The prediction interval is actually a measurement ranging from zero to one that compares the 30-year values observed by each station with the ones predicted from the model. In this manner, we are able to capture any large, medium or low 30-year climatic variability that occurred in approximately the last 100 years.

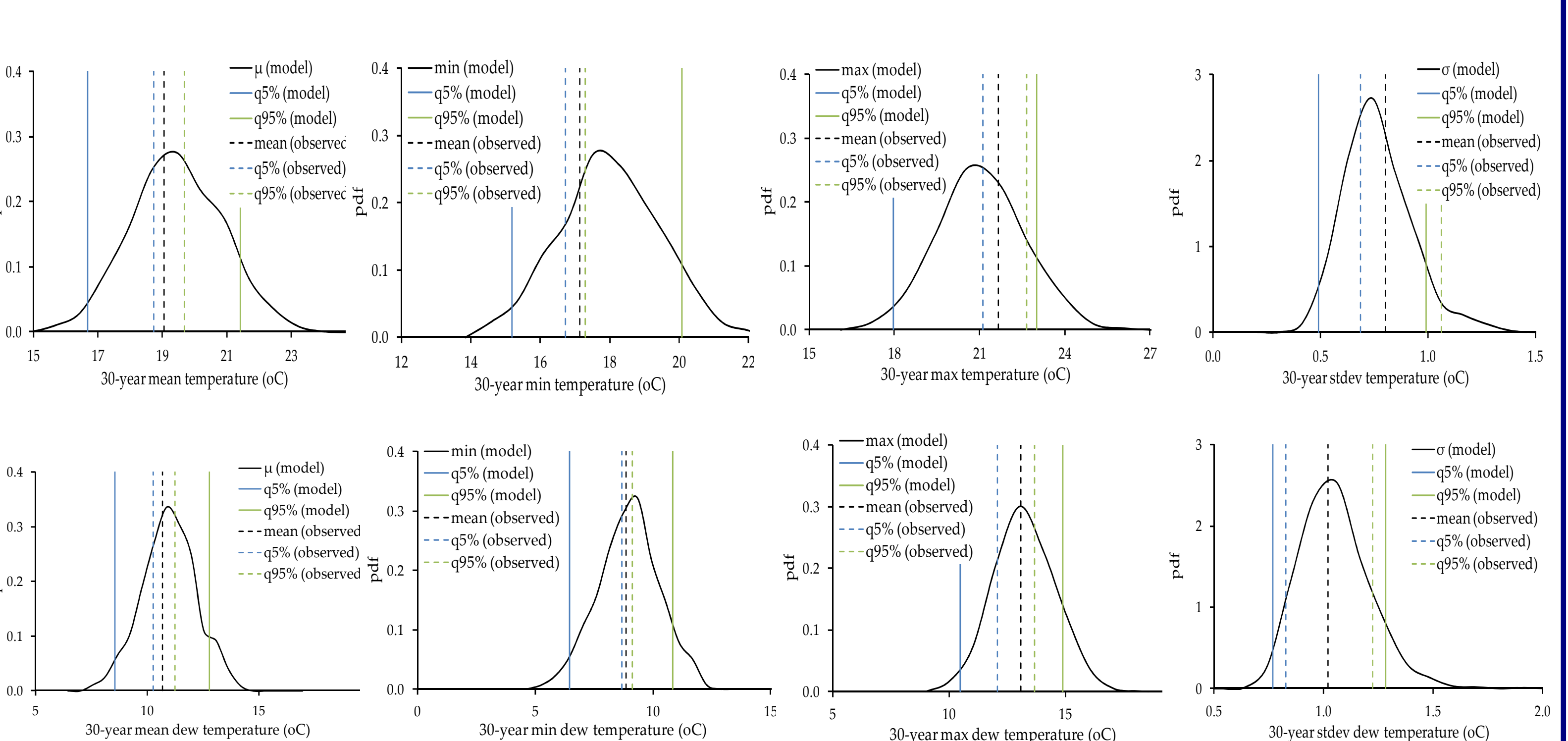
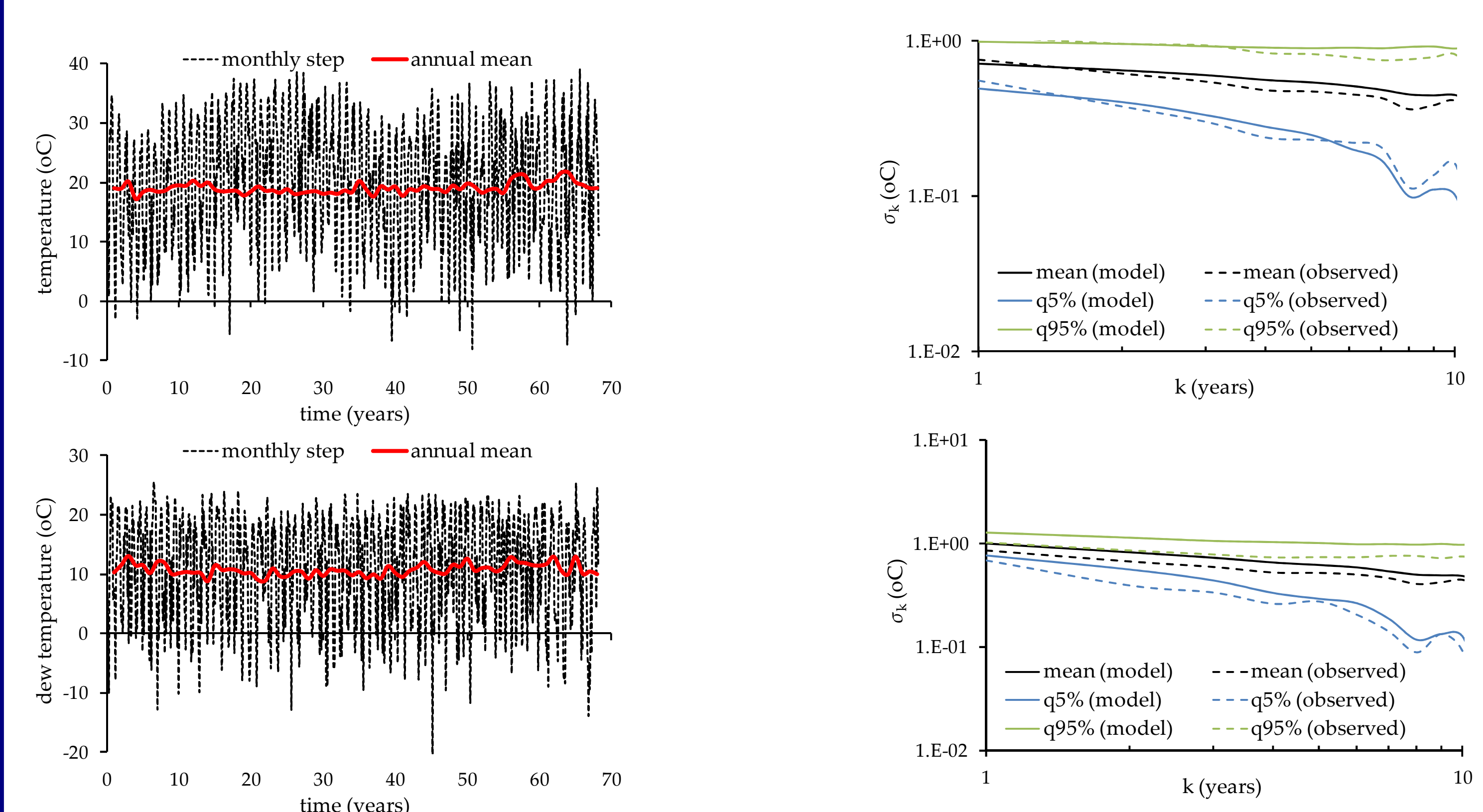


| Köppen-Geiger climate classification | Swy D/T   | Sye D/T   | nSwy D/T | maxs D/T  | mins D/T    | meanS D/T   | Hurst coefficient D/T | Location D/T                                                 |
|--------------------------------------|-----------|-----------|----------|-----------|-------------|-------------|-----------------------|--------------------------------------------------------------|
| AF                                   | 1973/1973 | 1934/1942 | 42/42    | 29,39/39  | -11,17/17   | 22,32/38,82 | 0,63/0,83             | Parham, Antigua and Barbuda/Parham, Antigua and Barbuda      |
| Am                                   | 1973/1973 | 1914/1914 | 42/42    | 28,9/36,7 | -3,7/10,7   | 19,24/48,86 | 0,77/0,83             | Miami, USA/Miami, USA                                        |
| As                                   | 1939/1939 | 1914/1914 | 76/76    | 27/43,4   | -5,1/1,7    | 18,32/24,76 | 0,74/0,76             | Honolulu,Hawaii/Honolulu,Hawaii                              |
| Aw                                   | 1945/1945 | 1914/1914 | 70/70    | 31,7/39,7 | -0,1/1,7    | 20,82/26,59 | 0,83/0,88             | Guantanamo,Cuba/Guantanamo,Cuba                              |
| Bwk                                  | 1973/1973 | 1934/1942 | 42/42    | 34,5/39   | -36,4/-30   | -1,83/12,32 | 0,61/0,80             | Nevada,USA/Nevada,USA                                        |
| Bwh                                  | 1973/1973 | 1934/1942 | 42/42    | 30,5/3    | -39,7/-30   | 9,24/48,86  | 0,56/0,86             | Toronto,Toronto,Toronto,Toronto                              |
| Bsk                                  | 1943/1943 | 1934/1942 | 72/72    | 28,34/22  | -38,3/-15,6 | 10,72/17,11 | 0,81/0,77             | Los Angeles,USA/San Diego,USA                                |
| Bsh                                  | 1948/1948 | 1914/1914 | 67/67    | 27,8/48,3 | -27,8/-19,4 | 8,8/18,58   | 0,68/0,84             | Texas,USA/Texas,USA                                          |
| Cfa                                  | 1943/1943 | 1934/1942 | 72/72    | 29,34/33  | -22,7/-17,7 | 10,64/19,01 | 0,76/0,84             | Dallas,USA/Dallas,USA                                        |
| Cfb                                  | 1941/1941 | 1934/1942 | 74/74    | 24,3/33   | -33,3/-19,8 | 4,5/7,77    | 0,82/0,66             | Metlakatla,Canada/Metlakatla,Canada                          |
| Csa                                  | 1945/1945 | 1914/1914 | 70/70    | 21,1/20   | -1,4/-5,0   | 9,8/16,91   | 0,81/0,69             | Kodiak Island by Alaska/Kodiak Island by Alaska              |
| Csb                                  | 1973/1973 | 1934/1942 | 42/42    | 27/38     | -26,9/-12   | 8,61/15,03  | 0,84/0,96             | Montpellier,France/Montpellier,France                        |
| Csc                                  | 1947/1947 | 1934/1942 | 68/68    | 26,1/31,3 | -3/0        | 13,5/17,48  | 0,81/0,74             | Terceira Island,Portugal/Terceira Island,Portugal            |
| Cwa                                  | 1973/1973 | 1934/1942 | 42/42    | 29/47     | -38,7/19,8  | 6,28/22,08  | 0,34/0,91             | Incheon,South Korea/Incheon,South Korea                      |
| Cwb                                  | 1973/1973 | 1934/1942 | 42/42    | 33/50     | -42,3/-3,4  | 17,09/28,08 | 0,88/0,92             | Chiapas,Mexico/Chiapas,Mexico                                |
| Dfa                                  | 1945/1945 | 1914/1914 | 70/70    | 26,3/38   | -37,8/-24,4 | 4,42/10,79  | 0,84/0,68             | Boston,USA/Boston,USA                                        |
| Dfb                                  | 1949/1949 | 1934/1942 | 66/66    | 26,38/39  | -35,2/-29,4 | 4,68/10,59  | 0,82/0,72             | Pittsburg,USA/Pittsburg,USA                                  |
| Dfc                                  | 1942/1942 | 1934/1942 | 73/73    | 22,3/31,1 | -51,7/-44,4 | -2,24/3,31  | 0,88/0,77             | King Salmon,Alaska/King Salmon,Alaska                        |
| Dsa                                  | 2002/2001 | 2003/2013 | 13/13    | 21,24/3,5 | -33,7/-19,9 | -0,44/13,24 | 0,76/0,6              | Hamadan,Iran/Savay, Kyrgyzstan                               |
| Dsb                                  | 1998/1998 | 1914/1914 | 13/17    | 19,36     | -33,3/-28,2 | -2,24/2,93  | 0,81/0,87             | Idaho,USA/Idaho,USA                                          |
| Dsc                                  | 1983/1983 | 1934/1942 | 13/13    | 23,34/9   | -51/53      | 11,55/16,38 | 0,87/0,79             | Pruthie,Alaska/Pruthie,Alaska                                |
| Dwb                                  | 1946/1946 | 1914/1914 | 69/69    | 30,2/32   | -39,2/-21,6 | 3,08/10,83  | 0,58/0,81             | Seoul,South Korea/Khalgodi,Mongolia                          |
| Dwc                                  | 1992/1992 | 1934/1942 | 23/23    | 26,3/39,4 | -38,7/-4,4  | -1,85/-0,12 | 0,33/0,56             | Huizhinen,China/Hanguo,North Korea                           |
| Dwd                                  | 1945/1945 | 1934/1942 | 72/72    | 28,4/32   | -55,4/-46,7 | -9,95/-3,32 | 0,62/0,65             | Mageda Gagin Sijidao,near Mongolia and Russia/Turun,Mongolia |
| ET                                   | 1983/1983 | 1914/1914 | 74/74    | 14,6/21   | -19,8/-13,2 | 2,7/13,14   | 0,77/0,81             | Barrow,Alaska/Barrow,Alaska                                  |

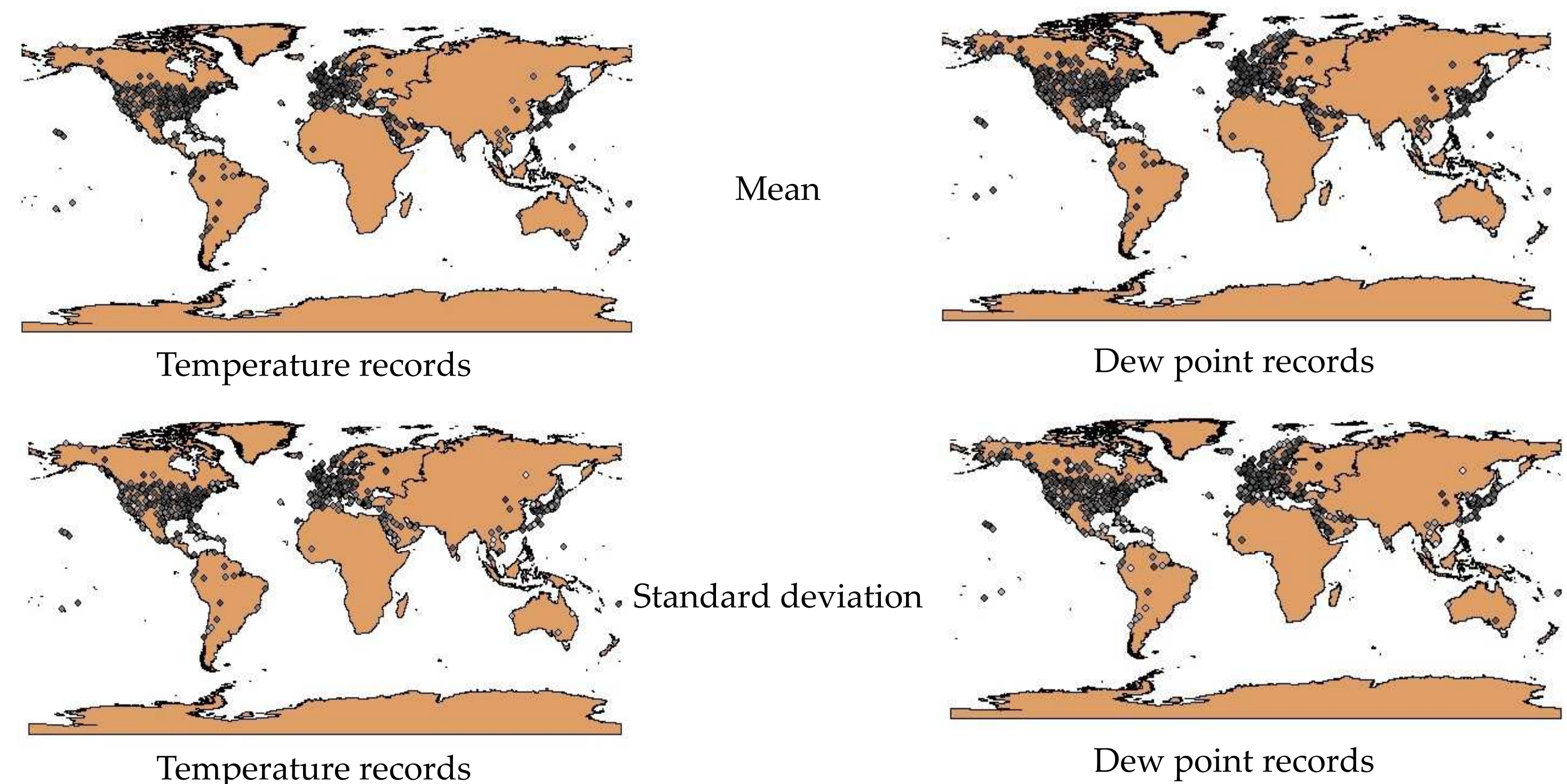
The table above illustrates some of the characteristics of the examined meteorological stations for dew point and temperature records, based on two criteria. First, a grading is estimated based on the Köppen-Geiger climate classification for each station. Then, the station of higher credibility for each Köppen-Geiger climate classification is selected, based on the criterion of at least 30 continuous years of observations (nSy). An important comment is that most of the reliable stations are found in the USA. The orange cells indicate the meteorological stations for dew point and temperature records located at the same Köppen-Geiger climatic classification, but in a different location.



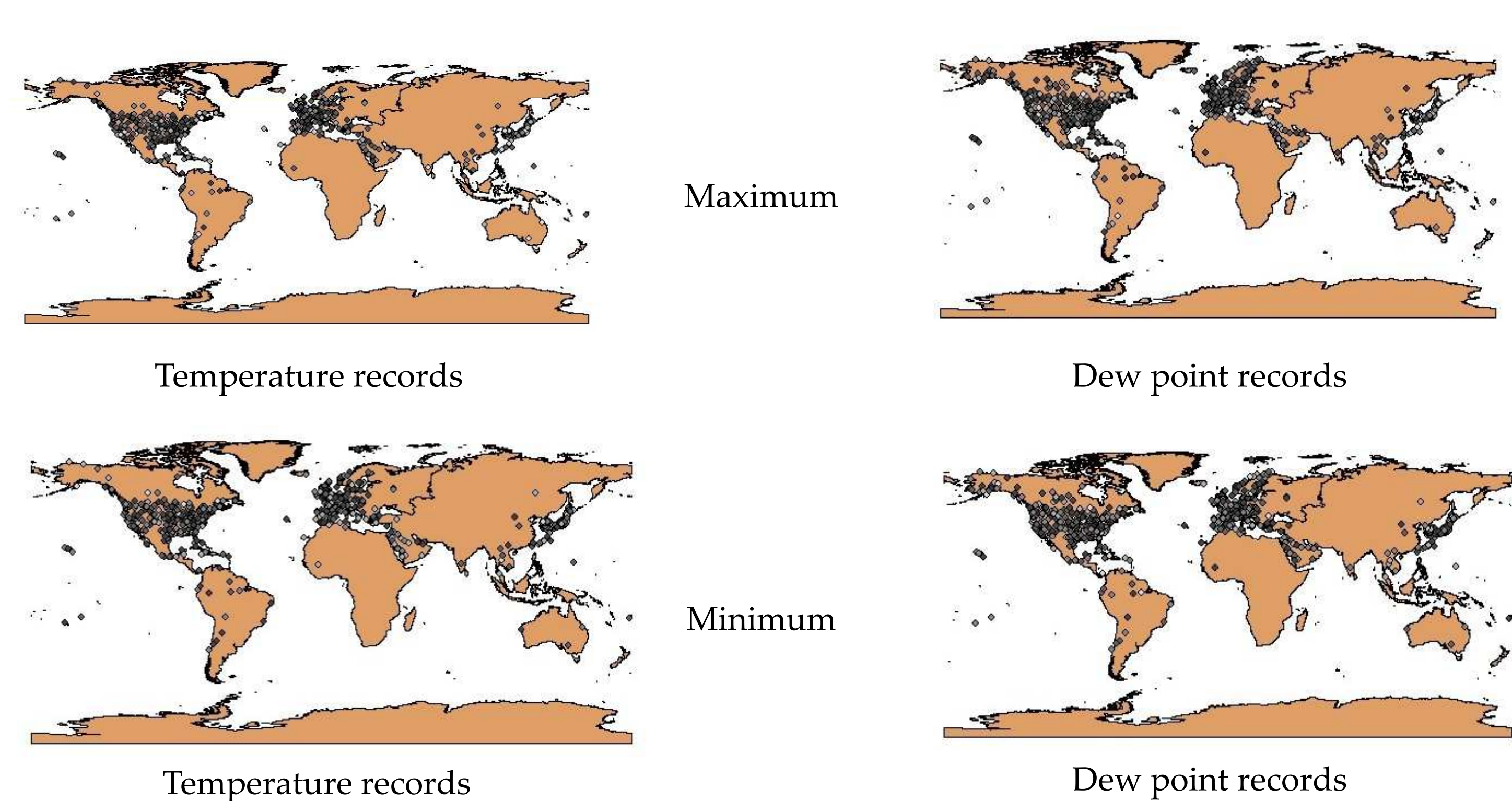
We observe that the Hurst coefficient is larger at the warm temperate zones, where the mean temperature and dew point records are higher. This may be explained that at these zones the clustering effect is more intense.



It seems that the Fractal Gaussian Noise model we are using has an adequate prediction interval.



As the values increase from zero (0) to one (1), the dots turn from white, to grey and finally to black. The mean temperature prediction intervals vary from 0.74 to 0.99, while the standard deviation prediction intervals from 0.09 to 0.99. The mean dew point prediction intervals vary from 0.56 to 0.99, while the standard deviation ones from 0.07 to 0.99. For both temperature and dew point records, more than 50% of the standard deviation values are larger than 0.70.



As the prediction intervals increase, the dots turn from white (corresponds to zero prediction interval), to grey and finally to black (corresponds to prediction interval equal to 1). The maximum temperature prediction intervals vary from 0.08 to 0.99, while the minimum ones from 0 to 0.99. The mean dew point records vary from 0.07 to 0.99, while the standard deviation ones from 0 to 0.99.

- The prediction intervals of the mean values of the temperature and dew point records are all larger than 0.8. Therefore, the HK model (or else Fractional Gaussian Noise) we adopt, can adequately predict the climatic variability of the examined processes.
- Prediction measures of the standard deviation, maximum and minimum values of both records, vary from 0.07 to 0.99, but the majority of them is larger than 0.65, as shown in the previous slides.
- We observe that as the mean value of temperature and dew point records increase, the corresponding value of the standard deviation decreases. This phenomenon mostly emerges at the warm temperate zones. Also, the Hurst coefficient at these zones was estimated higher than 0.85.

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