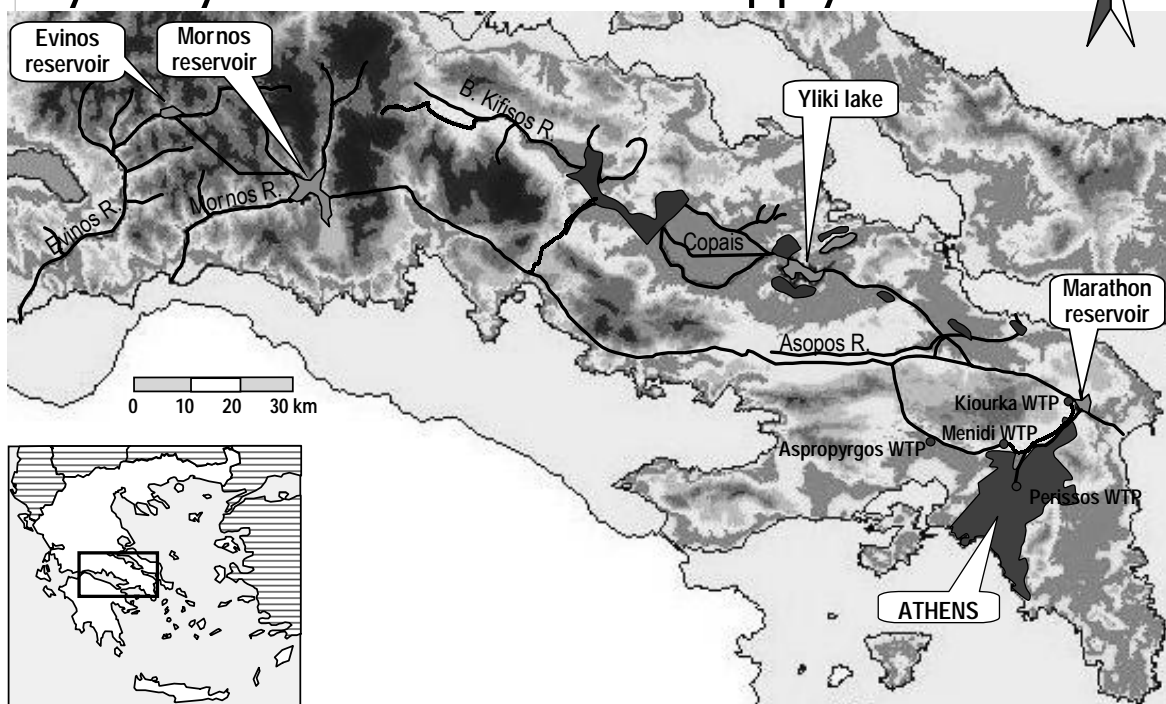


A stochastic hydrology framework for the management of multiple reservoir systems

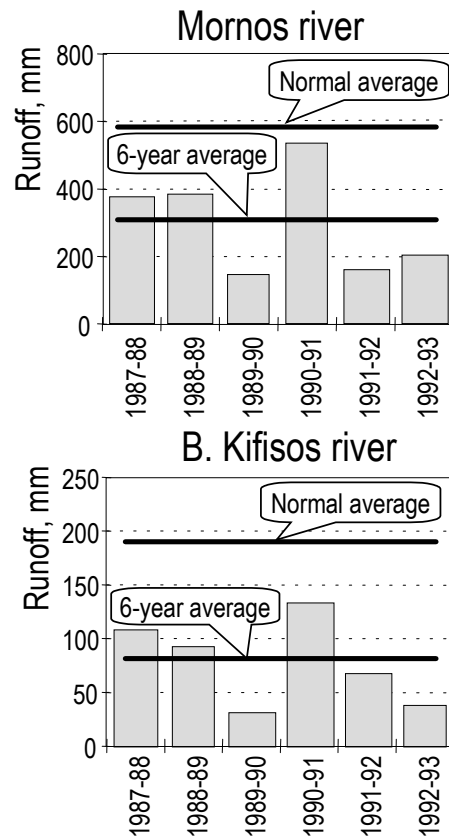
Demetris Koutsoyiannis & Andreas Efstratiadis
Department of Civil Engineering, National Technical University, Athens

Motivation: The management of the hydrosystem for the water supply of Athens



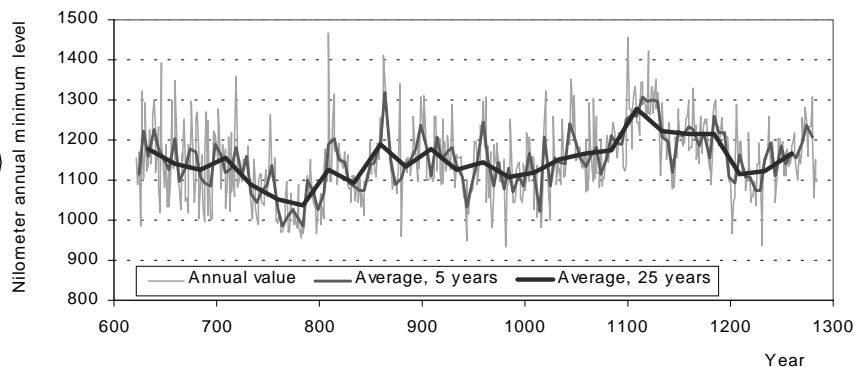
Requirements for stochastic simulation

1. Multivariate model
2. Time scales from annual to monthly or sub-monthly
3. Preservation of essential marginal statistics up to third order (skewness)
4. Preservation of joint second order statistics (auto- and cross-correlations)
5. Capturing/reproduction of "patterns" observed in the last severe drought – Preservation of long-term persistence

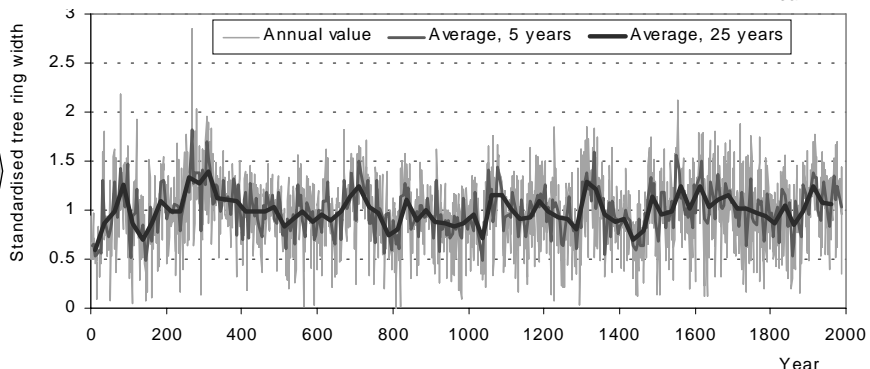


Climatic persistence versus climatic variability

Annual minimum water level of the Nile river for the years 622 to 1284 A.D. (663 years)
Hurst exponent = 0.85



Standardised tree ring widths from a paleoclimatological study at Mammoth Creek, Utah, for the years 0-1989 (1990 years)
Hurst exponent = 0.75



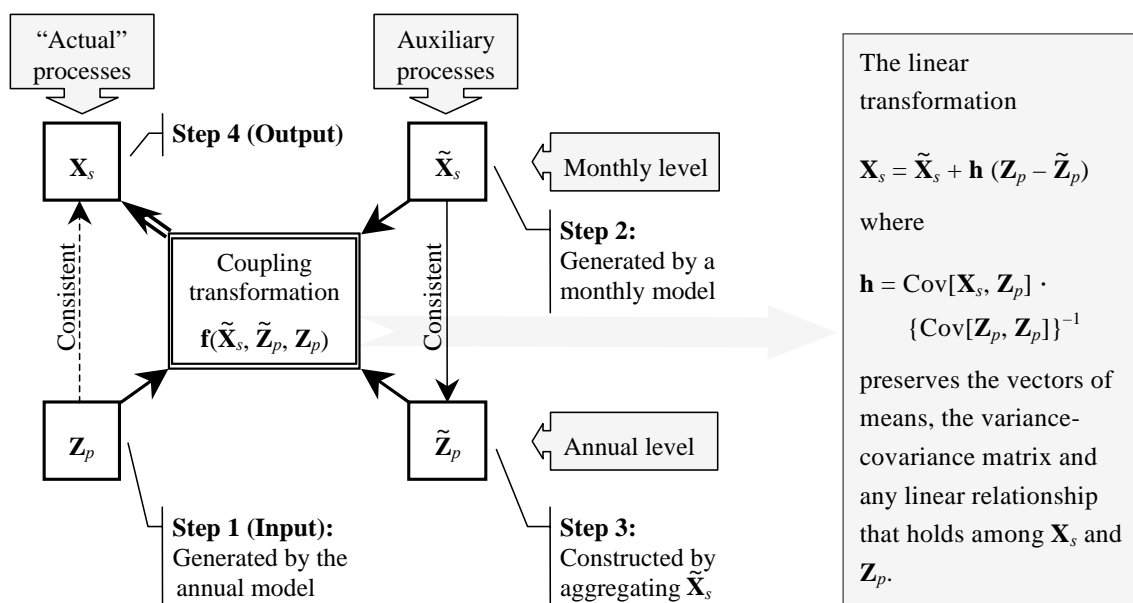
Methodology 3: Stochastic simulation in forecast mode

- ◆ In terminating simulations of a hydrosystem the present and past states must be considered.
- ◆ The observed values of the present and past must condition the hydrologic time series of the future.
- ◆ This is attainable using a two-step algorithm
 1. Generate future time series without reference to the known present and past values.
 2. Adjust future time series using the known present and past values and a linear adjusting algorithm.
- ◆ The linear adjusting algorithm:
 1. is expressed in terms of covariances among variables;
 2. preserves exactly means, variances and covariances;
 3. is easily implemented.

See details in: Koutsoyiannis, D., A generalized mathematical framework for stochastic simulation and forecast of hydrologic time series *Water Resources Research*, 36(6), 1519-1534, 2000.

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Methodology 4: Coupling stochastic models of different time scales



See details in: Koutsoyiannis, D., Coupling stochastic models of different time scales, *Water Resources Research*, 37(2), 379-392, 2001.

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Methodology 5: Preservation of skewness in multivariate problems via appropriate decomposition of covariance matrices

- ◆ Consider any linear multivariate stochastic model of the form

$$\mathbf{Y} = \mathbf{a} \mathbf{Z} + \mathbf{b} \mathbf{V}$$

where \mathbf{Y} : vector of variables to be generated, \mathbf{Z} : vector of variables with known values, \mathbf{V} : vector of innovations, and \mathbf{a} and \mathbf{b} : matrices of parameters.

- ◆ The parameter matrix \mathbf{b} is related to a covariance matrix \mathbf{c} by

$$\mathbf{b} \mathbf{b}^T = \mathbf{c}$$

- ◆ This equation may have infinite solutions or no solution.
- ◆ The skewness coefficients $\boldsymbol{\xi}$ of innovations \mathbf{V} depend on \mathbf{b} .
- ◆ The smaller the values of $\boldsymbol{\xi}$, the more attainable the preservation of the skewness coefficients of the actual variables \mathbf{Y} .
- ◆ Therefore, the problem of determination of \mathbf{b} can be solved in an optimisation framework, that combines
 - minimisation of skewness $\boldsymbol{\xi}$, and
 - minimisation of the error $\|\mathbf{b} \mathbf{b}^T - \mathbf{c}\|$.
- ◆ A fast optimisation algorithm has been developed for this problem.

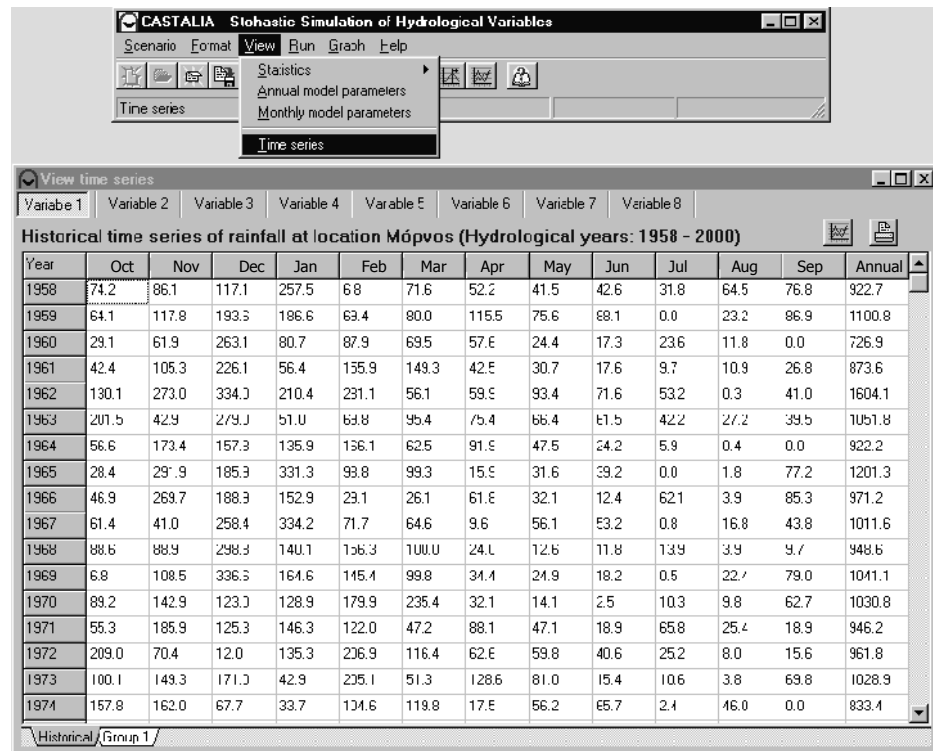
See details in: Koutsoyiannis, D., Optimal decomposition of covariance matrices for multivariate stochastic models in hydrology, *Water Resources Research* 35(4), 1219-1229, 1999.

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Implementation of the methodology: The **Castalia** software

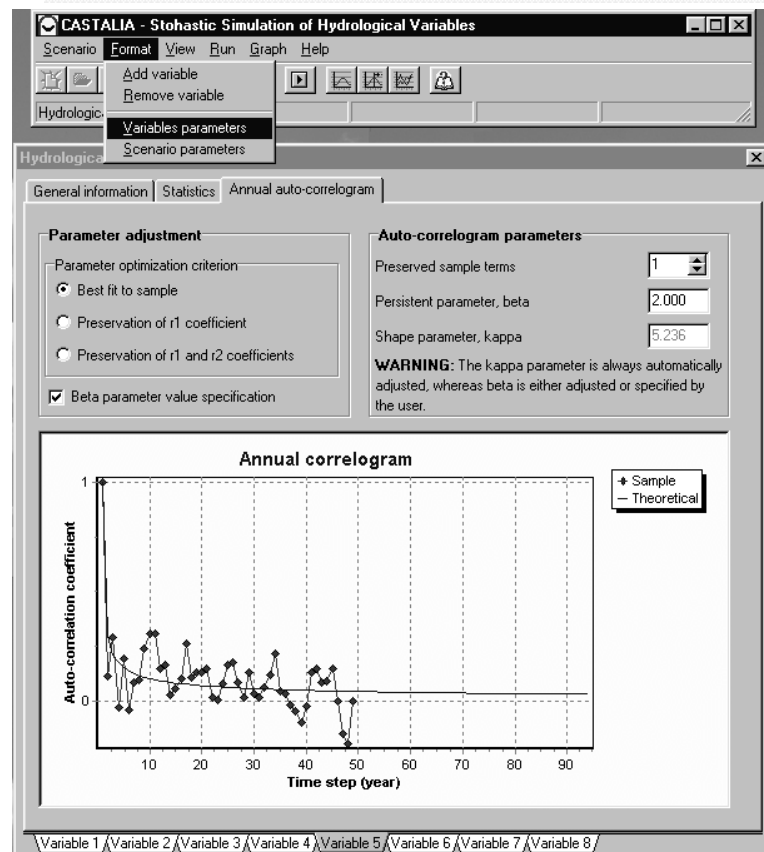
- ◆ Designed as part of a decision support system for the water resource system of Athens
- ◆ Linked to a simulation-optimisation model of a hydrosystem
- ◆ Can also perform as a stand-alone software
- ◆ Written in **Delphi**; utilises **Oracle**.
- ◆ Simulates several hydrological variables at multiple sites
- ◆ Uses annual and monthly time scales
- ◆ Preserves:
 - essential marginal statistics up to third order (skewness)
 - joint second order statistics (auto- and cross-correlations)
 - long-term persistence

Castalia: Data base operations for time series



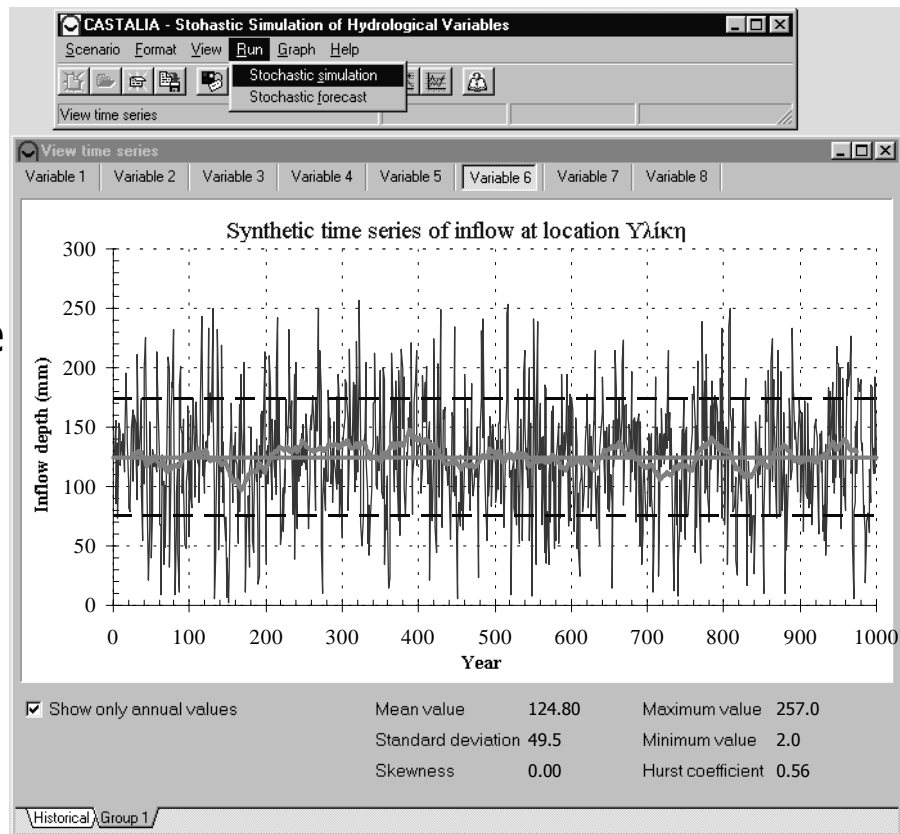
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Castalia: Parameter estimation- Parameters of autocorrelation and persistence



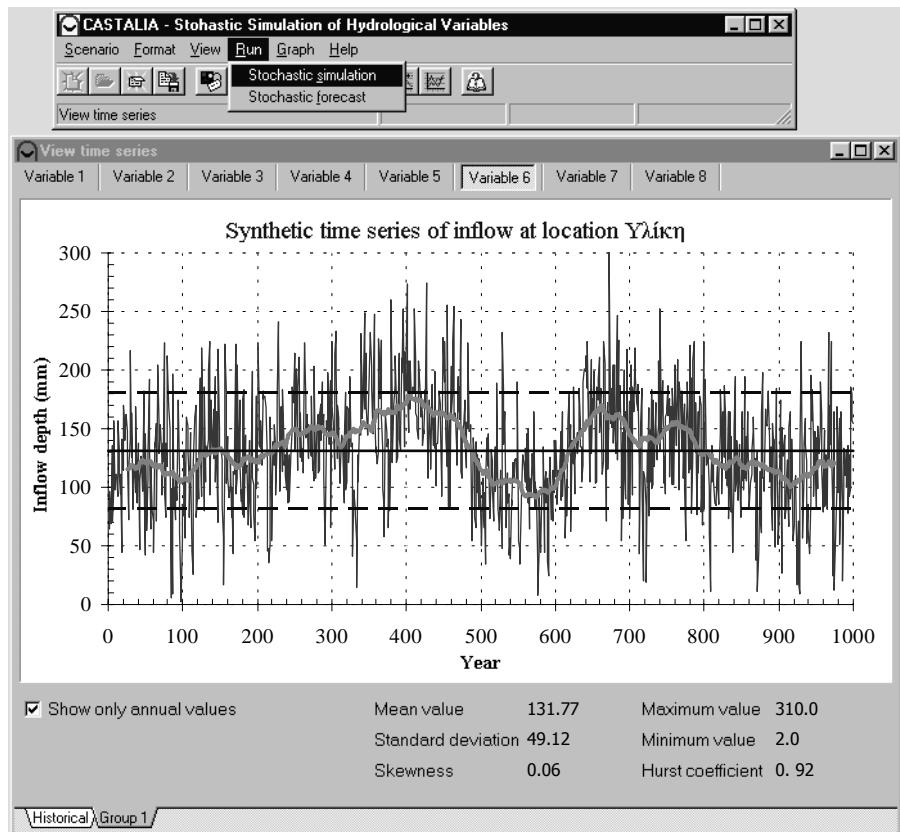
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Castalia: Stochastic simulation without long term persistence



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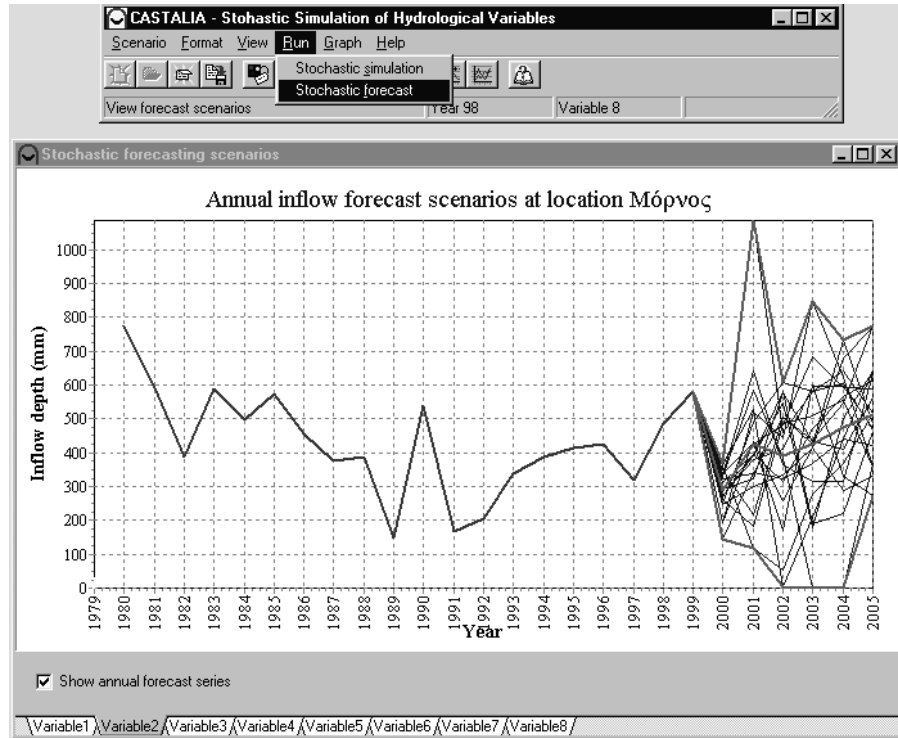
Castalia: Stochastic simulation with long term persistence



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Castalia:

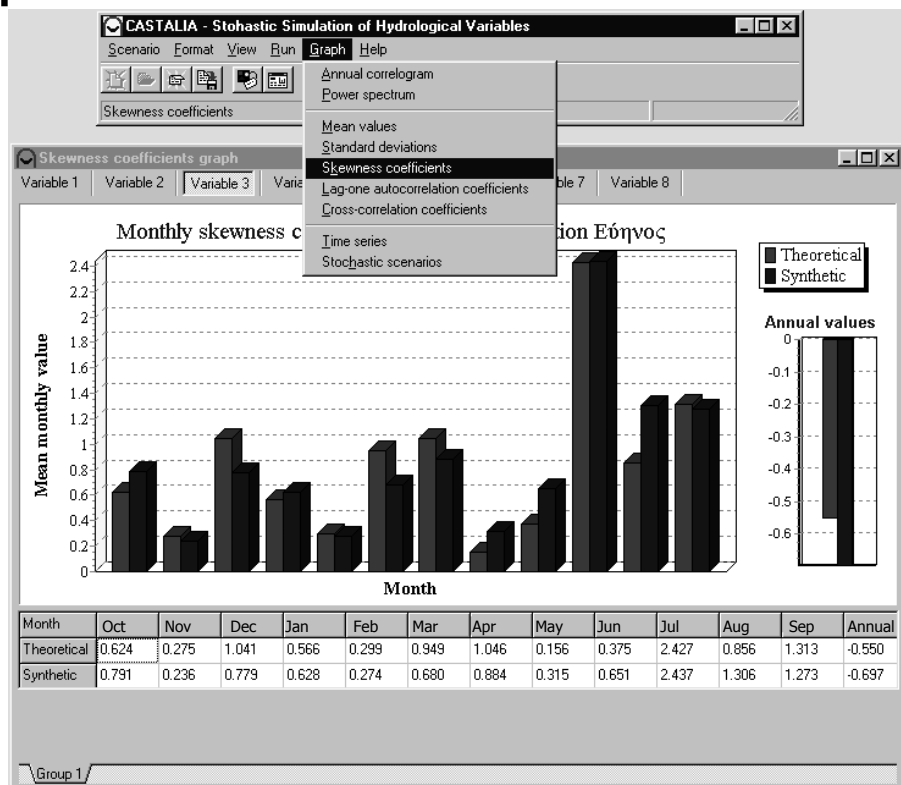
Stochastic forecasting with long term persistence



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Castalia:

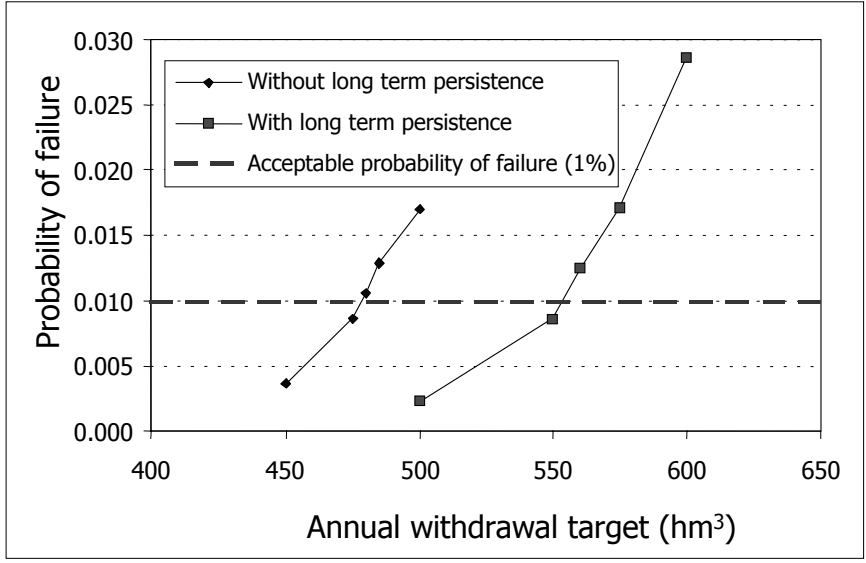
Preservation of marginal statistics – Skewness



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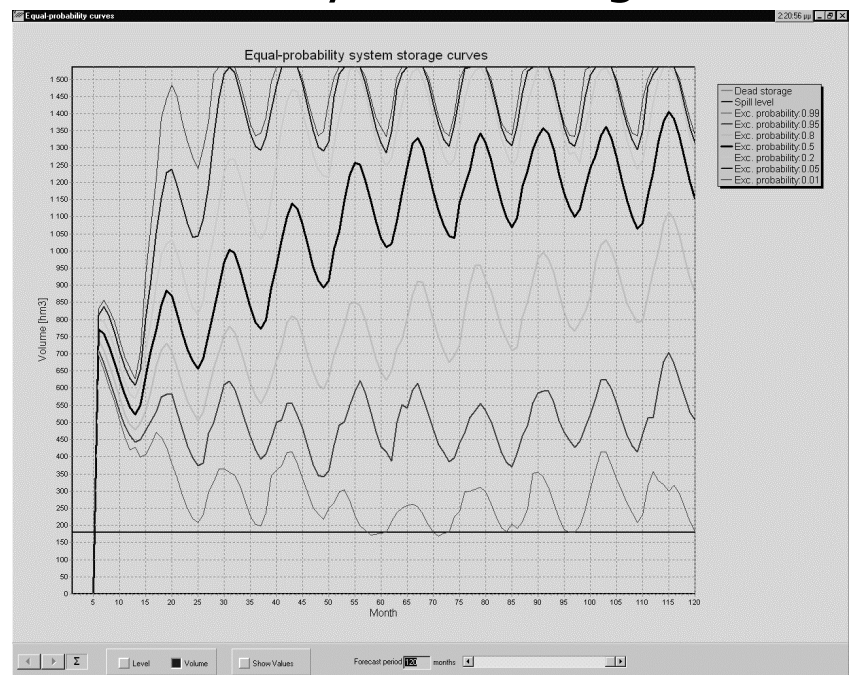
Utilisation of Castalia's results in the hydrosystem of the Athens water supply: System's firm yield

Results of steady-state simulations for 2000 years with and without long-term persistence



Utilisation of Castalia's results in the hydrosystem of the Athens water supply: Stochastic forecast of system storage

Evolution of quantiles of system storage (for several levels of probability of exceedance) for the next 10 years as a result of 200 terminating simulations with long-term persistence



Summary

- ◆ A generalised stochastic modelling framework for hydrological variables has been developed.
- ◆ The methodology involves the combination of novel stochastic techniques, and preserves long-term persistence and asymmetric distributions in multivariate, sequential or disaggregation, problems.
- ◆ The methodology has been implemented in the **Castalia** program.
- ◆ The methodology and the program have been tested in a large hydrosystem involving 4 hydrologic catchments with 4 reservoirs.